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WIND-TUNNEL MEASUREMENTS
OF PERFORMANCE, BLADE MOTIONS,
AND BLADE AIR LOADS FOR
TANDEM-ROTOR CONFIGURATIONS
WITH AND WITHOUT OVERLAP

by Robert J. Huston
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SUMMARY

Results of an investigation in the Langley full-scale tunnel of the performance, blade motions, and instantaneous blade air loads are presented for two tandem-rotor configurations for a range of tip-speed ratios from 0 to 0.28. The results indicate that the induced power requirements of tandem-rotor helicopters are generally predictable on the basis of the span loading of the blade-swept area. Interference effects on lateral rotor tilt, at transition tip-speed ratios contribute yaw-trim changes with speed, aside from yaw-trim changes due to unequal torque to the front and rear rotors. Air-loads measurements on the rear rotors of the tandem configurations indicate that the vortices generated by the blades of the front rotor significantly affect the azimuth variation of the air loads on the rear rotor.

INTRODUCTION

The aerodynamic performance of a helicopter with tandem rotors is affected by mutual interference between rotors. This mutual interference results in an unequal distribution of specific power (horsepower per pound of thrust) between rotors and affects blade motions and blade loads.

Investigations of the power requirements of tandem rotors have been made for some specific conditions (refs. 1 to 4). The flow field of tandem rotors has been studied both theoretically and experimentally (refs. 4 to 8) with regard to predicting the interference power increments, blade motions, and stability effects. The results presented in this report are intended to supplement and extend the previously published information.

The present paper presents measured power and blade motions for both rotors of two tandem-rotor configurations (nonoverlapped and highly overlapped) over a range of tip-speed ratios from 0 to 0.28. Presented as an appendix are measured blade loads (at five spanwise stations on the rear rotor) for each of the conditions investigated.

SYMBOLS

^a 0	constant term in Fourier series that expresses β ; hence, rotor coning angle, deg
al	coefficient of $-\cos\psi$ in expression for β ; hence, longitudinal tilt of rotor cone with respect to axis of no feathering, positive for rearward tilt, deg
⁸ 2	coefficient of -cos 2ψ in expression for β ; positive for upward flapping at $\psi = 90^{\circ}$ and 270° , deg
A_{O}	mean blade pitch angle at three-quarter radii, deg
b 1	coefficient of $-\sin\psi$ in expression for β ; hence, lateral tilt of rotor cone with respect to axis of no feathering, positive for tilt toward advancing side, deg
b ₂	coefficient of -sin 2ψ in expression for β ; positive for upward flapping at $\psi = 0^{\circ}$ and 180° , deg
c _{P,i}	induced power coefficient, $\frac{\text{Induced power}}{\pi R^2 \rho(\Omega R)^3}$
$\mathbf{c}_{\mathbf{T}}$	rotor thrust coefficient, $\frac{\text{Thrust}}{\pi R^2 \rho(\Omega R)^2}$
f	equivalent flat-plate area representing propulsive force, based on unit
	coefficient, Propulsive force , sq ft Free-stream dynamic pressure
ı	instantaneous section lift, lb
ı _o	steady term in Fourier series for section lift, lb/in.
l_n	coefficient of $\cos(n\psi + \phi_n)$ in series for section lift, lb/in.
L	instantaneous total blade lift, lb
L _O	steady term in Fourier series for total blade lift, lb
L _n	coefficient of $\cos(n\psi + \Phi_n)$ in series for total blade lift, lb
n	harmonic order
q	free-stream dynamic pressure, lb/sq ft

- r radial distance to blade element, ft
- R blade radius measured from center of rotation, ft
- V free-stream velocity, ft/sec
- x distance between rotor shafts, ft
- α rotor tip-path angle of attack; angle between projection in plane of symmetry of shaft axis and line perpendicular to flight path, positive rearward, deg
- blade flapping angle, with respect to axis of no feathering at particular azimuth position $(\beta = a_0 a_1 \cos \psi b_1 \sin \psi a_2 \cos 2\psi b_2 \sin 2\psi \dots)$
- μ tip-speed ratio, $\frac{V \cos \alpha}{\Omega R}$
- ρ mass density of air, slugs/cu ft
- ϕ_n phase angle, with respect to zero azimuth, of amplitude of nth harmonic of section lift, deg
- Φ_n phase angle, with respect to zero azimuth, of amplitude of nth harmonic of total blade lift, deg
- X wake skew angle, deg
- ψ blade azimuth angle measured from downwind position in direction of rotation, deg
- Ω rotor angular velocity, radians/sec

APPARATUS AND TESTS

The tests were conducted in the Langley full-scale tunnel which is fully described in reference 9.

The rotor configurations tested are shown in figure 1. The rotors, in all cases, were identical in planform with a radius of 7.625 feet, a constant chord of 1.16 feet, and an NACA 0012 airfoil section. The solidity was 0.0968. The blades were mounted on teetering hubs with zero built-in coning.

For the tandem configurations, the rotor blades were phased 90° apart. As viewed from above, the front rotor rotated clockwise and the rear rotor, counterclockwise. The spacing between hubs was varied to give an overlapped configuration (x/R = 1.23) and a nonoverlapped configuration (x/R = 2.03). A large ground board was mounted 2.04 radii below the rotors.

The thrust and torque of each rotor were measured independently by using strain-gage instrumentation located in each rotor support. Blade-flapping and blade-feathering motions, with respect to the rotor shaft, were sensed by strain gages and recorded on an oscillograph. Blade flapping with respect to axis of no feathering, was determined from these measurements. The overall accuracies of the data are estimated to be as follows:

Thrust				•			•	•	•	•	•	±9 lb or 2%
Torque							•		•	•	±4	ft-lb or 1%
Rotor tip speed											±1	fps or 0.2%
Flapping and feathering motions												±0.25 deg

All tests were conducted at a tip speed of approximately 500 fps, which corresponds to a tip Reynolds number of 3.7×10^6 in hovering. The rotors were always trimmed for zero flapping with respect to the shaft; thus both rotors of the tandem configurations were maintained in the same plane. The rotors on the tandem configurations were maintained at the same thrust. (Thrust, in this case, is defined as the force along the shaft axes.)

The measured power requirements of all rotors were adjusted to zero parasite drag on the basis of the measured longitudinal forces on the entire model; that is, the power was corrected for the longitudinal components of the rotor resultant force. These longitudinal, or propulsive forces, were corrected for rotor-off tares. The power correction was calculated as the power required to produce the propulsive force at the test airspeed. For the power requirements of the individual rotors of the tandem configurations, the power correction was equally divided between the two rotors.

Calculations of the jet-boundary effects, according to reference 10, indicated that only at the lowest forward-flight speed was the correction significant with respect to the accuracy of the data. At the lowest forward-flight speed ($\mu=0.075$), the angle-of-attack correction for the nonoverlapped tandem was determined to be 0.8°. However, considering the individual rotors, the correction for the front rotor was 0.06° while that for the rear rotor was 1.4°. Because of this ambiguity, the data, even for this tip-speed ratio, are not corrected for jet-boundary effects.

The forward-flight results presented in this investigation were obtained by using the same tandem-rotor model as that used to obtain the hovering results of reference 2.

RESULTS AND DISCUSSION

The comparisons of performance and blade motions between single rotor and multirotor configurations, included in this paper, are intended to aid in identifying interference effects. It must be clearly understood that the comparison of the aerodynamic efficiency of the configurations, on the basis of the presented power-required curves, assumes a specific set of conditions. These conditions will not be compatible in a series of configurations (single and multirotor) all

designed for the same mission. The important consideration is that the ingredients of a power-required curve for the different configurations be shown to be predictable.

Power Requirements

The level-flight power requirements of the two tandem configurations and the single-rotor configuration are presented in figure 2 as nondimensional power-to-thrust ratio for a range of tip-speed ratios. (This ratio is, for the single rotor, the more familiar ratio of power coefficient to thrust coefficient.) The results presented are for zero parasite drag and at constant thrust per rotor ($C_T = 0.0043$ for each rotor, matched within the accuracy of the measurements), hence keeping the mean blade load constant throughout the speed range. The hovering performance and blade motions were obtained from reference 2.

Hovering.— It is noted that the nonoverlapped tandem (x/R=2.03) requires the same specific power (power per pound of thrust) as the single rotor in hovering. In contrast, the overlapped tandem (x/R=1.23), at the same mean blade load, requires about 8 percent more total power, which (assuming all the increase to be in the induced portion of the power) corresponds to about 13 percent more induced power. Of this 13 percent, about $7\frac{1}{2}$ percent can be attributed to the increased disk loading based on the swept area of the overlapped tandem. The remaining $5\frac{1}{2}$ —percent increase in induced power must be attributed to flow interference within the overlapped area. Had the disk loading been equal to that of the nonoverlapped tandem, this $5\frac{1}{2}$ —percent increase in induced power would have represented a total power increase of about $3\frac{1}{2}$ percent. It is shown in reference 2 that the twin-rotor hovering-power requirements (including the effect of interference) can be adequately predicted by either the methods of reference 4 or 5.

Forward flight. In forward flight, the specific power required by the rear rotor of both configurations exhibits a substantial increase between hovering and a tip-speed ratio of 0.075. This increase results in the total specific power, at this tip-speed ratio, being nearly the same as that in hovering. Another interesting result is that the total specific power of the overlapped configuration (x/R = 1.23), at the higher tip-speed ratios, becomes nearly equal to (actually slightly less than) the specific power requirements of the nonoverlapped configuration (x/R = 2.03). Considering that the swept-area disk loading of the overlapped configuration is 15.6 percent greater than that of the nonoverlapped configuration (since front and rear rotors carried the same thrust in all cases), this fact appears to contrast with normal expectations. The flow studies of reference 6 indicate that the explanation for these results appears to lie in the flow field experienced by the rear rotor of tandem configurations. This flow field apparently results in an increase in the induced power requirements on the rear rotor.

One method suggested for predicting the induced power requirements of the rear rotor of a tandem is to determine the mean value of the induced velocity of the front rotor acting upon the rear rotor (from charts such as those given in ref. 11), and to add this velocity to the rear-rotor induced velocity to determine the induced-plus-interference power requirements. The results of such a computation are given in figure 3(a) for the rear rotor of the nonoverlapped configuration. The computations were made with due regard for the effect of the interference velocity on the rear-rotor induced velocity. The experimental induced-power data (shown by the symbols) were determined by assigning the tandem configurations the same profile power-to-thrust losses as the single rotor for, logically, any real change in the profile power of one rotor due to the proximity of a second rotor should be attributed to interference. It is seen from figure 3(a) that the computation seriously underestimates the actual rear-rotor induced-plus-interference power requirements.

Another method is suggested by the theory that predicts the induced power requirements of a single-rotor helicopter. The induced power requirements of a single-rotor helicopter can be reduced to

$$\frac{C_{\mathbf{p,i}}}{C_{\mathbf{T}}} = \frac{\mu(\text{Lift})}{\pi \sigma(\text{Span})^2} \tag{1}$$

for certain limits of angle of attack and tip-speed ratio. The same result is obtained from simple wing theory by considering the span loading. This result suggests a comparison of the measured induced and interference power to an induced power calculated on the basis of the span loading of the configuration. Inasmuch as the exact expression for the induced power of a single rotor machine is:

$$\frac{c_{p,i}}{c_{T}} = \frac{\mu(\text{Lift})}{\pi q(\text{Span})^2} \left(\frac{\sin x}{\cos 3\alpha}\right)$$
 (2)

it appears that equation (2) is a more useful equation for general use.

The results of calculations made by using equation (2) to predict the induced power requirements are given in figure 3(b) for the two tandem-rotor configurations. Inasmuch as the lift and dynamic pressure are the same for both configurations, at the same tip-speed ratio, the two configurations have the same calculated induced power. The experimental data agree reasonably well with the calculated performance. The results indicate that the power requirements of tandem-rotor helicopters, with longitudinal spacing between the two limits of this investigation, can be adequately predicted by this method.

The distribution of power between the front and rear rotors appears to be predictable by assigning the front rotor the induced power requirements of a single rotor and assigning the rear-rotor induced power requirements three times that of a single rotor (fig. $\mathfrak{Z}(a)$). The average induced power of the tandem configurations, with such a division of power, is as predicted by the span loading.

Blade Motions

Measured first-harmonic blade flapping, over the tip-speed range, is presented in figure 4. There appears to be little net interference effect between rotors, or effect of longitudinal spacing, on the longitudinal tilt (all flapping) of the tandem configurations. The longitudinal tilt of the tandem-rotor configurations does show a slightly steeper slope with tip-speed ratio than that of the single rotor.

The significant interference effects on lateral tilt (b_1 flapping) of the rotors on the tandem configuration occur below a tip-speed ratio of 0.2. This can be noted by comparing the front and rear rotor flapping of the tandem configurations with that of the single rotor. The b_1 flapping of the single rotor is the result of blade coning (involving blade bending) and the self-induced time-average longitudinal variation of induced velocity across the rotor.

The b_1 flapping of the front rotor of the nonoverlapped tandem is only slightly affected by the rear rotor. This effect is greatest in hovering and at tip-speed ratios above transition speeds ($\mu=0.04$ to 0.08). However, the front rotor lateral flapping of the overlapped tandem is substantially larger than that of the single rotor, below a tip-speed ratio of 0.2, and has approximately the same magnitude as the b_1 flapping of the nonoverlapped tandem at the higher tip-speed ratios. The lateral flapping of the rear rotors of both tandems is reduced substantially, at low tip-speed ratios, from that of the single rotor. The primary result of the tandem-rotor interference effects on lateral tilt is to contribute changes in yaw trim with speed, aside from yaw-trim changes due to unequal torque to front and rear rotors.

Three sources for the interference effects on b_1 flapping are possible. First is the interference contribution to the time-average longitudinal variation of induced velocity across the rotor. Estimates of this effect, based on the charts of reference 11, indicate that this effect increases b_1 flapping for the front rotor of the overlapped tandem, and decreases the b_1 flapping for the rear rotors of the tandem configurations. In addition, the predicted b_1 flapping, due to the longitudinal variation of induced velocity, would be a maximum in the transition region ($\mu = 0.04$ to 0.08) with negligible lateral tilt contributed at the higher tip-speed ratios. However, while the predicted trends agree with the trends of the measured data, the magnitude of the predicted b_1 flapping is inadequate to account for the flapping interference.

The second and third sources of the interference effects on the lateral tilt of the tandem rotors are the result of interference effects on steady-state blade coning (a_0) and second harmonic flapping (a_2) . (Both a_0 and a_2 , for the teetering rotor used in this investigation, occur as blade bending.) Changes in a_0 and a_2 on the tandem rotors, differing from those resulting on the single rotor, result in an interference-induced change in the lateral tilt of the rotors. The effect of a_0 and a_2 on lateral tilt increases with tip-speed ratio but would be negligible in hovering. Because the large interference effects on lateral flapping appear in hovering and throughout the transition region (where

the effect of a_0 and a_2 on b_1 is small), the principal source of the effect is attributed to the interference contribution to the time-average longitudinal variation of induced velocity across the rotors.

The blade collective pitch required to obtain constant thrust per rotor is given in figure 5 for all configurations investigated. The corresponding rotor tip-path-plane angle of attack and resulting total propulsive force, in square feet of drag area, are also given in figure 5. The propulsive force of the tandem configurations would be expected to be twice that of the single rotor; however, the data of figure 5 indicate that the procedure used in setting the test conditions resulted in somewhat greater than twice the propulsive force.

Air Loads

The rear-rotor air loads, for all conditions previously discussed, are presented in the appendix. The air-loads data are included to provide designers of tandem-rotor helicopters with quantitative measurements of the exciting forces on a rotor blade operating in the wake of an adjacent rotor. This information is required for a rational analysis of sources of vibration excitation, thereby leading to a structural design free of dynamic and fatigue problems.

The pressure measurements indicate an additional complication to the problem of predicting theoretical air loads for tandem-rotor helicopters. It is shown, experimentally and theoretically in references 12 and 13, that the variation of air loads around the azimuth, for a single-rotor helicopter, is affected by the relative location of the blades with respect to previously generated vortices from adjacent blades. Limited examination, in the light of the results of reference 12, indicates that rear-rotor air loads are more strongly affected by vortices generated by the front rotor than by vortices generated by the adjacent blade of the same rotor, at least for the conditions of this investigation. The effect of the forward rotor can be determined by comparing, at the same tip-speed ratio, the single-rotor air loads of reference 14 with the air loads of this investigation. This effect, as a function of the amount of overlap, can be studied from comparisons of the section loading, blade loading, and the harmonic analysis of the air loads of the two tandem configurations.

CONCLUDING REMARKS

The results of a wind-tunnel investigation with two tandem-rotor configurations, with equal thrust per rotor, indicate that the induced power requirements of tandem-rotor helicopters are generally predictable on the basis of the span loading of the configuration.

The effect of mutual interference on blade flapping is largest at high tip-speed ratios for longitudinal tilt but is largest at transition tip-speed ratios for lateral tilt. The interference effects on lateral tilt will contribute yaw-trim changes with speed, aside from yaw-trim changes due to unequal torque to the front and rear rotors.

The results of the air-loads measurements on the rear rotor of the tandem configurations indicate that the vortices generated by the blades of the front rotor significantly affect the azimuth variation of the rear-rotor air loads.

Langley Research Center,
National Aeronautics and Space Administration,
Langley Station, Hampton, Va., July 10, 1963.

APPENDIX

AERODYNAMIC LOADING ON THE REAR ROTOR OF THE TANDEM CONFIGURATIONS

EQUIPMENT

The equipment used in this investigation to measure the azimuth variation of the air loads is essentially the same as that used in references 14 and 15. The equipment is described in detail in the aforementioned references but is reviewed briefly here.

Rotor Blades

One blade of the two-bladed teetering rotor is instrumented to measure differential pressures between the upper and lower surfaces at 10 chordwise locations at each of 5 spanwise stations. Figure 6 is a sketch of the instrumented blade showing the principal dimensions and the pressure-orifice locations.

Pressure-Pickup Installation

The pressure pickups used are miniature electrical pressure gages (ref. 16) of a variable-inductance type. The overall frequency response for the pressure pickup-recording oscillograph system was determined to be flat to about 60 cycles per second, the sixth harmonic of rotor speed. There was a time lag in the system, independent of frequency, which amounted to 8° of azimuth.

Due to the limited number of sliprings available, simultaneous readings of all 50 pressure pickups were not possible. Therefore, with the use of a stepping switch, stations 1, 2, and 3 (at r/R = 0.31, 0.56, and 0.75, respectively) were recorded and then stations 3, 4, and 5 (at r/R = 0.75, 0.85, and 0.95, respectively) were recorded. Station 3 was thus recorded twice at each test condition as a check of the repeatability of the data and the compatibility of the inboard pressure measurements with the outboard pressure measurements. The second measurement of station 3 air loads is presented in the data as a flagged symbol.

TEST PROCEDURE AND DATA REDUCTION

Test conditions were set to the desired thrust per rotor and zero flapping, with respect to the rotor shaft, with model tare forces being taken into account. The shaft angles were predetermined for each test point in attempting to hold a constant representative flat-plate area.

The output of each pressure gage was recorded on an oscillograph and read at 48 points per revolution. The readings for corresponding points for

10 revolutions were averaged and recorded on automatic punch cards. Automatic computing machines then converted this average to a pressure differential and summed the output at each spanwise station to give the section loading. The section loading was then harmonically analyzed to give the amplitude and phase angle, with respect to zero azimuth, of each harmonic of loading. A correction for the time lag in the instrumentation described previously was then introduced. The values of section loading, when plotted against radius, were manually integrated to give total blade lift at 24 points per revolution. These data were then harmonically analyzed to give the amplitude and phase angle of each harmonic of total blade lift.

PRESENTATION OF RESULTS

Harmonic Analysis

The results of the harmonic analysis of the section blade lift and the total blade lift are given in tables I to IV. The section lift is presented as the first six harmonic terms in the harmonic series

$$l = l_0 + \sum_{n=1}^{n} l_n \cos(n\psi + \varphi_n)$$

The total blade lift is presented as the first six harmonic terms in the harmonic series

$$L = L_0 + \sum_{n=1}^{n} L_n \cos(n\psi + \Phi_n)$$

In order to make comparisons between different span stations and/or test conditions of the magnitude of the harmonics, the section lift is presented as a percentage of the steady-state mean blade loading (percent $L_{\rm O}/R$) as determined from the pressure measurements. In a similar manner, the harmonics of the total blade load are presented as a percent of the steady-state blade lift (percent $L_{\rm O}$).

Section Loading

The variation of section aerodynamic loading with azimuth is presented in figures 7 to 11 for the five radial stations. The data are presented in the following order:

Figu	re
Nonoverlapped tandem, hovering	
Total Blade Lift The variation of total blade lift with azimuth is presented in figures 12 to 16 in the following order:	
Figu	re
Nonoverlapped tandem, hovering	,

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TABLE I.- HARMONIC ANALYSIS OF MEASURED SECTION LOADING AND TOTAL BLADE LIFT IN HOVERING

در	φ _n , Lo deg		245 88 338 160 135		221 146 319 173 22 265		139 139 141 141 141 141	Ī	108 148 300 331 115 280
al lif	13			1		1	1 40040	1	1445048
Total blade lift	Lh, percent		100.00 .5 .7.8 6.1 6.1 1.6		0.001 0.00 0.00 0.00 0.00 0.00 0.00 0.0		100.0 17.3 16.5 6.3 8.1 11.6 7.8		100.0 6.1 15.2 4.6 6.1 8.7
95	Lo deg		538 106 338 182 72 140		319 139 309 171 171				
r/R = 0.95	$l_{\rm n}$, percent $\frac{L_{\rm o}}{R}$		274.0 37.7 26.3 14.1 9.4		246.2 16.7 12.5 16.5 16.5 10.7				
0.85	Lo deg		15 111 336 182 182 5		334 156 329 218 13		161 123 28 312 312 119		154 154 149 259 338 1111
r/R = 0.	l_n , $\frac{l_n}{Percent}$	1b	250 2.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1	1b	249.6 7.1 9.3 17.0 2.1 5.7	1b	299.2 5.0 14.0 16.5 32.4 23.7	q	281.4 8.1 34.5 3.3 18.2 28.0 16.5
75	Lo deg	168.4	173 87 340 147 299 609	232.0	1116 1143 3288 342 45	131.2	169 127 127 46 329 139	185.1 lb	183 152 332 341 129 283
r/R = 0.75 (repeat)	$\begin{pmatrix} \rho_n, & l_n, \\ R \end{pmatrix}$ deg percent $\frac{L_0}{R}$	$x/R = 2.03$; $L_0 = 16$	4.491 4.7.7 7.7.0 4.0 7.1.1	2.03; Lo = 23	176.9 3.6 6.0 6.0 7.8 1.9	23; L ₀ =	191.6 15.6 24.9 6.9 20.4 18.8 13.1	$\kappa/R = 1.25$; $L_0 = 18$	198.4 17.5 28.0 1.5 16.1 15.6
0.75	øn, deg	'R = 2	174 96 15 353 307	11	171 144 333 132 260 335	= 1.	169 146 6 335 138 295	- T	154 154 338 305 1117 315
r/R = 0.	$\begin{pmatrix} \rho_n, & l_n, \\ \frac{L_0}{R} & \text{deg percent} \end{pmatrix}$	/x	167.9 8.5 6.3 7.6 2.8 2.2	x/R	1.080 8.3 6.6 7.9 2.9 2.5	x/R	192.1 21.0 27.8 5.5 17.6 23.2 12.3	x/F	200.8 18.5 22.2 11.0 15.8 20.4 12.2
≥6	ϕ_{n} ,		1898 28 4 4 55		205 137 313 313 167 62 62		55 152 307 349 126 279		65 156 304 321 110
= 0.56									1 11 11 11 11 11
r/R	$\frac{\rho_{\rm h}}{R}$ deg percent		88.5 7.3 6.2 2.0 2.0 1.1 6.		96.0 9.1 5.2 2.8 2.8 2.2 1.7		85.8 8.3 16.6 7.9 7.7 4.2		78.9
0.31	For the second s		195 312 312 148 56		203 99 51 218 79 702		230 230 230 346		146 310 310 1190 349
r/R =	ln, percent		88.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.		9.7.0 4.7.0 1.0.1 2.0.1 2.0.1		20.6 9.5 11.5 11.5 6.1 1.4		23.2 6.4 12.7 9.6 7.2 1.2
	п		0101110		0101210		0107450		010250

TABLE II.- HARMONIC ANALYSIS OF MEASURED SECTION LOADING

AND TOTAL BLADE LIFT IN FORWARD FLIGHT

 $\left[x/R = 2.03\right]$

	r/R = 0	T	r/R = 0.56	5	r/R = 0.7	5	r/R = 0 (repes			r/R = 0.	85	r/R = 0.9) 5	Tot blade	rt		
n	l _n ,	$\frac{L_0}{R}$ deg	- 1	l_n , percent $\frac{L_0}{R}$	Øn, deg	L	!		$\frac{L_O}{R}$	1		ø _n ,	l_n , percent $\frac{L}{F}$	ø _n ,	L _n ,	L_{\circ}	$\Phi_{ m n}$, deg
						μ	= 0.	.075; Lo :	= 18 - T	1.2	lb				T		
0 1 2 3 4 5 6	14.3 17.9 7.9 4.3 3.6 1.9	350 350 26. 15. 5	5 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	103.3 20.0 12.9 .5 3.4 1.5	16 13 181 159 188 142	212.5 4.6 16.6 9.8 3.6 3.4 5.3	271 13 20 278 197 81	206.9 4.0 16.7 7.4 4.6 3.3 6.1		281 27 27 27 252 202 97	262.7 13.4 19.4 10.6 13.0 1.2 9.9	205 75 22 273 146 94			100.0 7.8 8.4 1.7 3.3 1.9 2.0	} ,	349 31 359 238 164 58
						L	μ = (0.10; L _o	= 18	3.6	1b						
0123456	19.2 18.7 9.5 .8 1.9 1.0	19 14	1 6 1 5 6	104.9 28.2 26.3 3.8 .6 1.8	13 359 217 276 143 185	209.9 1.6 34.8 5.9 6.0 4.4 8.6	56 355 9 329 222 117	36.6 10.8 5.7 5.7		140 350 7 324 258 102	277.3 13.6 13.0 18.4 22.0 2.5 18.8	190 19 4 306 219	45.1 8.0 16.7 12.3	228 101 285 305 128	8.2 15.1 2.1 4.2	2 + + 2 3	3 17 341 305 96 123
-					.	<u> </u>	μ =	0.14; L ₀	= 1	71.5	lb						
0 1 2 3 4 5 6	17.7 17.2 15.3 1.2 2.2 4.2	31 8	5	120.0 24.1 34.4 6.5 7.8 .7	14 348 317 255 40 227	48.8 27.1 8.1 6.3	58 333 331 238 217 255	52.0 24.9 9.1 8.9	?) ,	78 335 325 286 224 265	15.0 39.8	274 349 342 282 228	24.9 52.0 13.9 32.6 17.3	256 121 311 210 211 158	8.8 17.1 10.0 5.1 5.1	8 5 0 6 3	2 354 325 236 236 156
					-k	J	<u>μ</u> =	0.19; L ₀	= 1	95.8	lb						
0 1 2 3 4 5 6	16.9 10.1 6.3 1.7	35 1 1	 +0 58 32 18 98 78	108.9 17.3 46.2 15.7 2.0 1.7	50 357 62 124 142 58	9.2 62.6 33.1 7.3	297 342 16 14 44 143	5.8 55.3 22.6 9.6	5 5 6	318 346 3 325 195 179	27.6 39.4 6.1 17.0	330 350 344 344 286 120	18.4 11.0 1 32.3 14.4 8 15.1	289 240 348 30° 270 110	8. 23. 3 13. 7 1.	3 3 0 8 4	13 353 15 297 281 120
				-			μ =	0.24; Lo	= 1	89.3	lb						
0 1 2 3 4 5	10.6 12.6 12.2 2.4	311	77 42 40 38 62	117.3 19.0 50.1 15.8 3.0 2.3 3.7	101 344 103 255 104 189	30.6 52.5 32.1 9.1 15.0	33-345 345 110 33-149	27.9 5 45.5 4 27.1 5 6.1 15.9	9 5 3 7 9	353 344 16 136 334 143	53.6 32.6 38.2 10.8 19.7	33 34 10 31 13	3 29.9 5 14.2 9 30.1 8 .6 14.8	29 5 34 27 29 12	8 10. 0 24. 6 9. 5 3. 5 5.	1 3 0 1 2	6 348 25 98 328 138
	<u> </u>	١					μ=	0.28; Lo	= 1	76.5	5 lb			- 1			
0 1 2 3 4 5 6	11.9 25.6 3 17.9 4 4.9	1 3 1 1	08 26 31 83 47 91	65.7 18.1 9.8 4.1	111 32' 8: 18(20) 20	48.5 7 70.6 1 50.5 0 22.9 15.6	33/ 33/ 35/ 12/ 33 13	6 42.6 0 50. 3 52. 4 14. 3 13.	8 9 0 0 4	338 318 323 83 311 140	58.0 39.7 69.3 1 18.2 1 16.8	33 32 31 7 30 15	9.1 15.1 40.7 1 8.8 3.6	30 4 31 7 23 22	0 10. 1 32. 0 13. 3 5. 3 2.	.5 .9 .8	21 329 348 116 309 154

TABLE III. - HARMONIC ANALYSIS OF MEASURED SECTION LOADING AND TOTAL BLADE LIFT IN FORWARD FLIGHT FOR SPECIAL CONDITIONS

 $[x/R = 2.05; \mu = 0.19]$

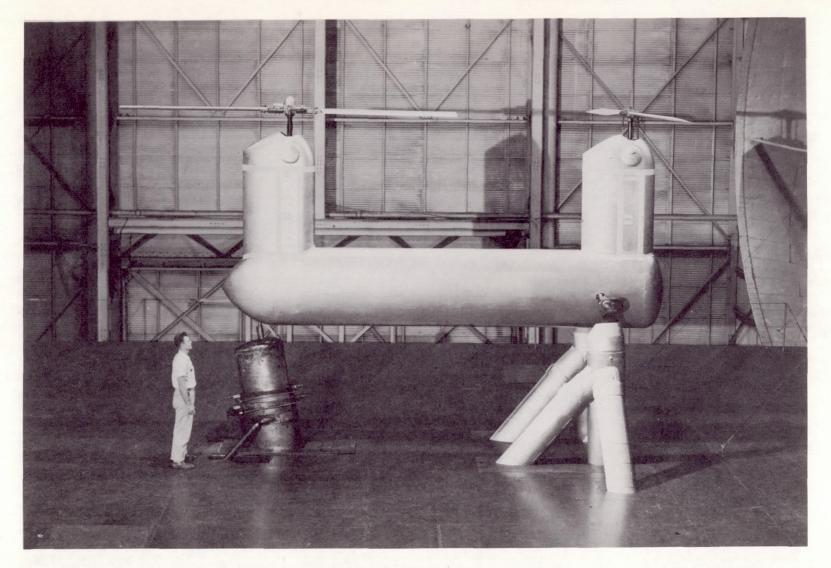
l t	Φ _n ,	deg		7	357 354 263 151		353	186 288 129		152	58 271 255 185
Total blade lift	$^{ m L_{n}}$	percent Lo		100.0 10.2 22.4	7.07.0		100.0	10.4.6.4 10.4.4.0.		100.0	17.0 4.0 1.9 4.8
	øn,			293	337 286 279 118		28	12 219 271 139		351	23 173 326 186
r/R = 0.95	eu 2	percent $rac{\mathrm{L}_{\mathrm{O}}}{\mathrm{R}}$		187.2 13.0 10.7	28.1 6.4 14.6 15.1		109.0	31.1 10.5 18.5			37.5 7.8 14.9 10.5
5	ø _n ,	gəp		340	15.7 15.4 16.5 16.5		322	135 283 127		353	35 210 323 197
r/R = 0.85	ln,	percent $\frac{L_0}{R}$: 234.9 lb	233.7 26.7 18.8	34.1 2.2 14.6 17.3	100.5 lb	277.1	34.1 13.3 37.4 5.4	3 1b	257.7 21.2 26.6	48.7 5.1 12.2 11.8
5	$\phi_{\rm n}$	deg	Lo =	327 341	345 334 174 187] 			192.3	303	77 297 174 233
r/R = 0.75 (repeat)	n,	percent Lo	6 lb/sq ft;	207.6 5.3 43.0	00 00 00 00 00 00 00 00 00 00 00 00 00	3 lb/sq ft;			= 100; Lo =	210.2 8.4 23.7	47.8 20.0 3.6 9.0
5	øn,	deg	ш	337	348 330 312 192	н	252 748	25 296 181 170	angle	257 65	59 218 171 228
r/R = 0.75	² ,u ²	percent Lo	Disk loading	212.1 6.1 48.9	26.7 10.8 1.9 9.2	Disk loading	224.6 2.1 59.1	30.8 9.8 5.3 10.5	Yaw an	208.7 7.2 16.1	48.5 18.3 8.8 10.0
9	ø _n ,	deg		-+ -1 349	38 322 217 332		71 359	72 170 82 21		15%	218 218 141
r/R = 0.5	ln,	percent R		118.1 12.3 47.3	10.0 2.3 1.3 2.0		128.4 15.7 47.3	2.5 2.5 2.5 2.5		107.4 15.5 24.1	15.7 6.2 6.3
0.31	ø _n ,	R deg	-	36	121 130 133 113		355 24	134 107 68 42		39	186 198 190 190
r/R = 0.	l 'u'	percent 1		23.1 16.4 13.3	7.0 2.8 1.5		4.1 13.0 16.5	8.3 6.1 2.3		18.4 19.3 8.2	7.8 8.0 8.0 8.0
	g .			010	m 4 m/o		010	M4 M0		0101	√4 √0

TABLE IV.- HARMONIC ANALYSIS OF MEASURED SECTION LOADING

AND TOTAL BLADE LIFT IN FORWARD FLIGHT

 $\left[x/R = 1.23\right]$

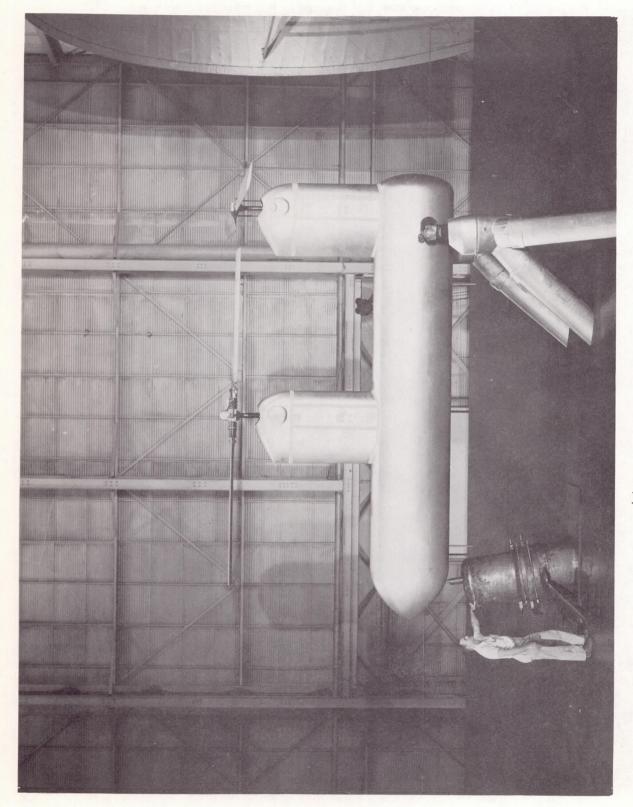
	r/R = 0	0.31	r/R = 0.56			,	r/R = (0.7 5		r/R = 0 (repea	0.75 at)	5	r/R = (0.85	5	r/R =	0.9	5	Total blade l	ift
n	l _n ,		ø _n , deg	l _n , percent	L _O	ø _n , deg	l _n , percent	L _O R	ø _n , deg	l _n , percent	L _o	ø _n , deg	l _n , percent	L _o	$oldsymbol{\phi}_{ ext{n}}$,	$l_{ m n}$, percent	L _o	ø _n ,	L _n , percent L	$\Phi_{ m n},$ o deg
	<u> </u>				1					.075; L _o =		L	L	•,		<u> </u>		1	<u> </u>	1,
0 1 2 3 4 5 6	10.9 36.2 3.4 5.3 3.8 4.0 3.4		8 69 254 37 150 252	111.1 56.5 20.8 9.0 10.6 3.2 4.7		10 350 196 335 140 216	225.1 3.7 48.6 31.5 25.1 4.8 6.8		306 335 148 330 157 192	227.4 6.2 48.8 28.5 21.9 7.0 6.6		282 331 142 338 153 185	417.5 18.4 24.8 95.3 137.8 31.1 38.6		214 19 149 311 131	89.3 17.7 12.8 43.0 59.5 7.1 18.9	7 3) -	80 354 148 313 96 108	100.0 29.2 15.6 15.8 10.9 5.6 6.5	18 353 196 348 338 162
	1	1			1			μ	= C).10; L _O =	= 18	32.7	lb			<u> </u>				1
0123456	11.6 33.5 8.8 2.6 4.7 5.1 3.6		13 40 336 39 131 210	107.5 38.5 34.1 6.3 9.6 2.9 3.9		9 347 205 325 113 203	200.2 1.6 73.3 23.4 23.0 6.6 7.2		0 536 145 330 147 210	203.8 2.1 71.2 24.8 18.8 7.6 7.1		322 35 142 333 139 203	276.6 12.8 51.9 34.0 41.1 10.0 18.2		215) 325) 119 312 179 121	214.3 15.3 12.4 56.3 103.4 13.3	3 3 1	189 35 143 306 105 114	100.0 16.2 25.1 10.3 18.1 4.0 5.9	8 346 149 328 91 140
	·							μ	= C	.14; L _O =	- 17	8.4	lb							
0123456	18.5 30.9 12.9 •5 7.9 7.0 3.3		21 47 14 32 99 178	123.5 34.4 43.4 7.2 15.8 4.4 6.4		21 253 186 313 100 183	217.5 11.4 79.7 5.2 27.5 10.5 11.3	-	14 339 152 293 100 195	216.7 10.6 80.9 8.2 26.3 8.5 13.0		5 341 138 296 96 204	272.7 13.4 63.6 26.4 57.7 13.7 27.5		250 334 88 301 151 157	146.9 7.2 16.8 49.6 139.7 23.4	3	350 52 147 307 160 116	100.0 14.8 31.1 10.3 26.8 6.2 11.4	16 351 134 308 110 155
								щ	= 0	.19; Lo =	= 19	4.0	lb							
0123456	15.7 25.1 8.9 2.7 8.4 9.0 4.5		24 36 184 357 74 148	113.9 22.1 48.2 10.7 12.6 10.8 7.8		47 347 108 317 53 153	198.8 9.5 64.1 8.0 26.2 9.2 15.4	-	334 330 62 297 82	197.0 10.0 58.9 5.6 25.2 8.1 15.2		352 331 99 303 97 177	248.8 8.2 55.3 5.6 34.7 8.2 16.4		 340 326 112 296 103 177	215.8 13.0 19.0 17.0 57.6 9.5 18.4)) 	215 332 117 304 177 153	100.0 10.5 26.8 5.2 16.3 7.4 8.0	35 337 156 315 98 167
								μ	= 0	.24; Lo =	- 19	4.6	1b					,		
0123456	17.3 21.0 7.8 11.7 11.7 10.3 6.1		30 21 194 340 68 139	116.2 26.6 49.9 18.2 12.4 15.1 12.2		70 350 113 309 44 132	198.4 17.2 60.8 20.4 19.9 12.6 21.3		329 344 94 332 66 161	200.0 15.6 58.8 20.6 15.3 12.4 22.6		344 342 93 329 65 158	248.9 23.2 56.3 14.4 17.7 8.8 17.6		327 343 85 324 105 153	200.0 7.5 31.1 17.2 37.8 10.2		298 359 132 315 127 164	100.0 12.6 28.1 8.0 13.3 9.5 9.0	35 344 120 328 80 159
								μ	= 0	.28; L _o =	16	5.4	1b							
0123456	9.9 25.3 22.4 28.8 8.5 12.7 13.3		43 324 160 326 18 155	130.5 33.8 67.3 20.1 17.4 16.2 14.3		70 340 115 282 17	236.6 33.2 92.1 20.7 16.6 12.7 16.0		343 343 80 345 54 144	214.2 29.1 90.6 15.3 16.6 15.1		338 338 82 336 33 123	278.3 41.1 82.9 10.2 22.6 12.3 12.2		322 336 100 326 47	110.1 43.0 57.5 49.1 81.5 5.5 22.8		336 1 171 319 99 93	100.0 21.2 46.5 15.2 17.4 7.2 9.3	20 340 136 322 37 143



(a) Nonoverlapped tandem. x/R = 2.03.

L-95189

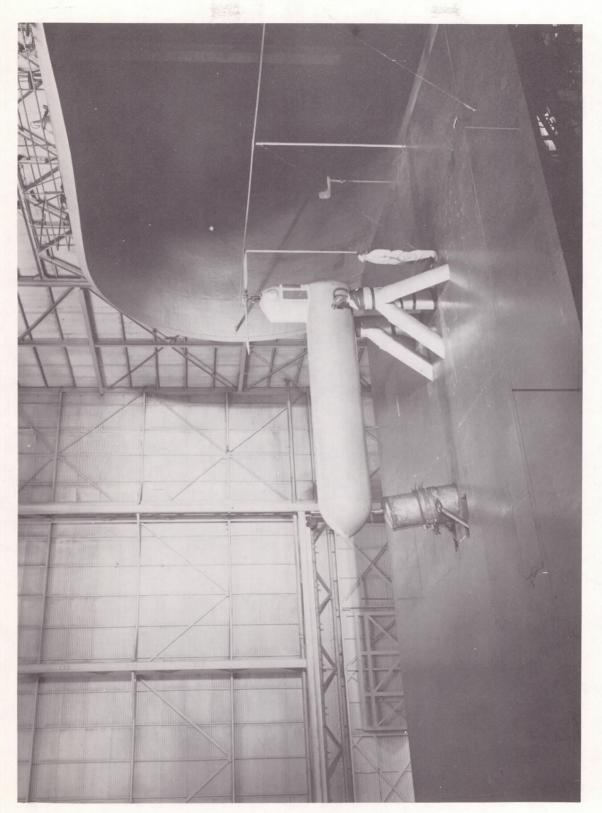
Figure 1.- Helicopter model in Langley full-scale tunnel.



(b) Overlapped tandem. x/R = 1.25.

Figure 1.- Continued.

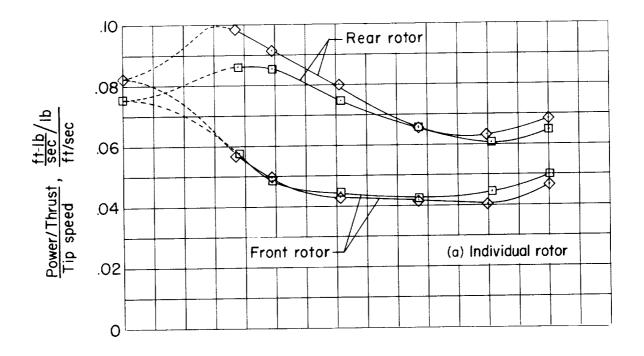
L-95399



(c) Single rotor.

L-57-2389

Figure 1.- Concluded.



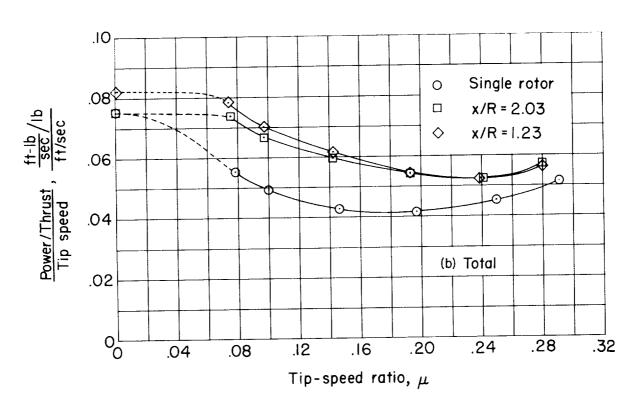
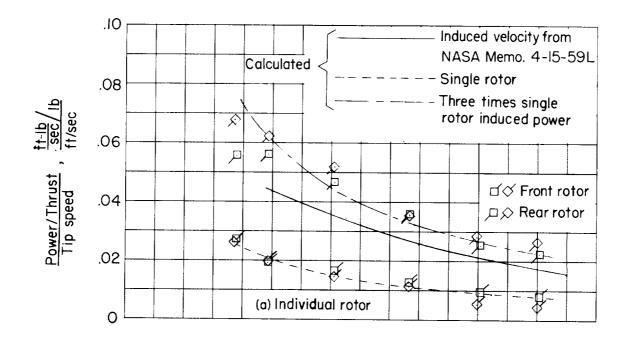


Figure 2.- Level-flight power requirements of tandem- and single-rotor configurations. $C_{\rm T}$ = 0.0043 (each rotor); zero parasite drag; hovering points from reference 2.



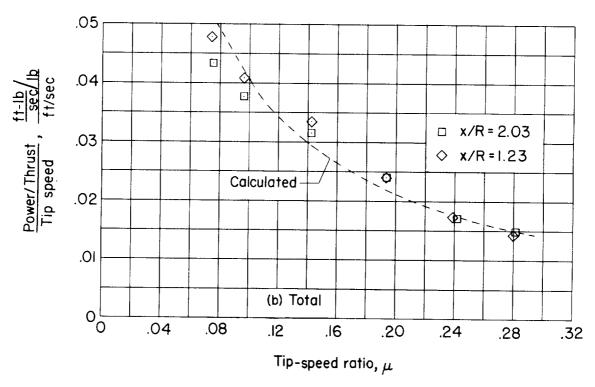


Figure 3.- Induced-plus-interference power requirements of tandem configurations. $C_{\rm T}$ = 0.0043 (each rotor).

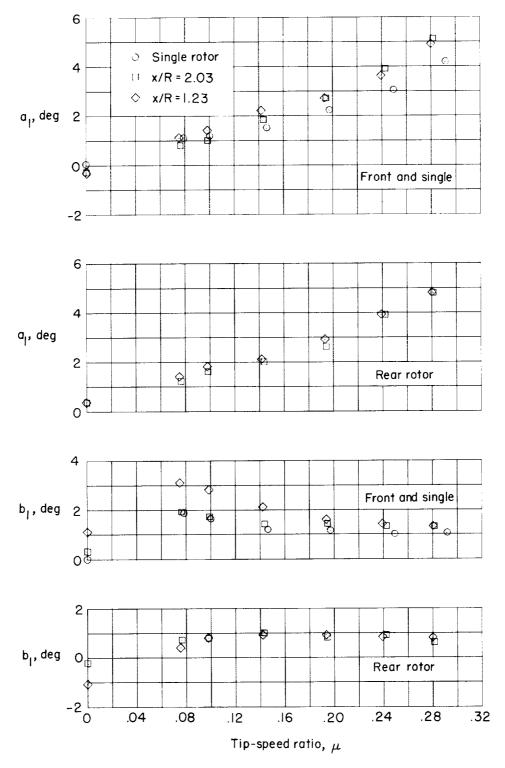


Figure 4.- Longitudinal and lateral flapping of tandem- and single-rotor configurations. $C_{\rm T}$ = 0.0043 (each rotor); hovering points from reference 2.

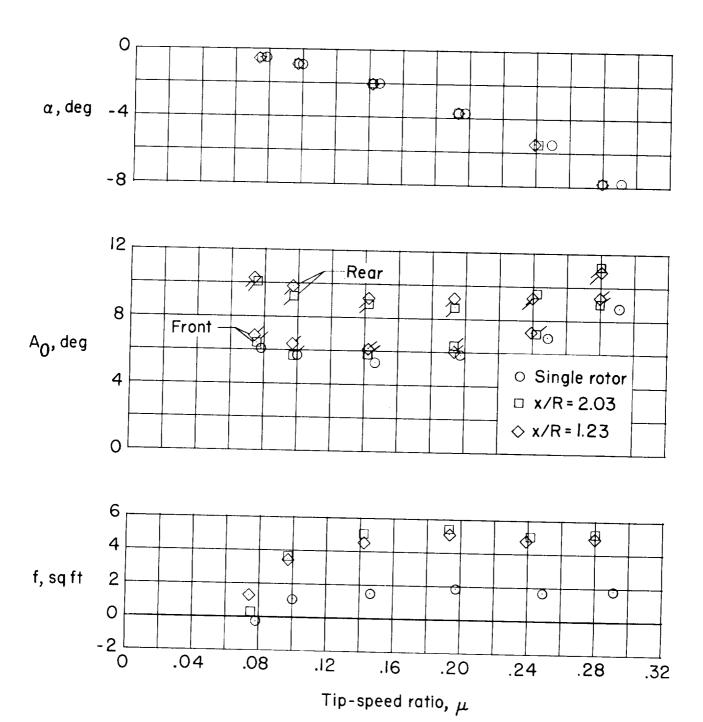


Figure 5.- Tip-path-plane angle of attack, mean blade pitch, and propulsive-force flat-plate area for tandem- and single-rotor configurations.

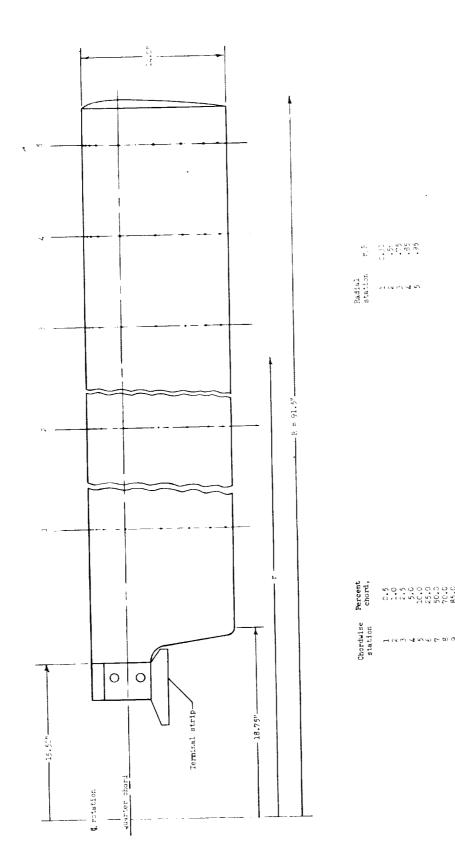


Figure 6.- Blade layout showing location of pressure orifices. Airfoil section, NACA 0012; rotor solidity, 0.097.

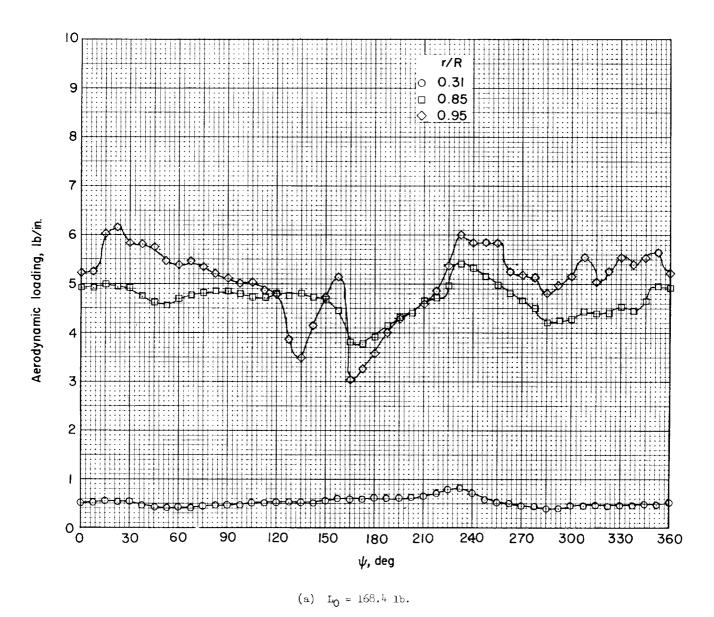
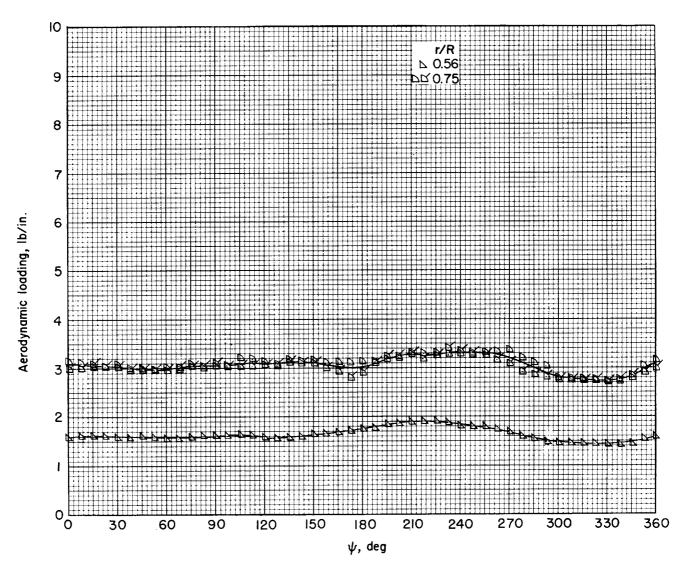
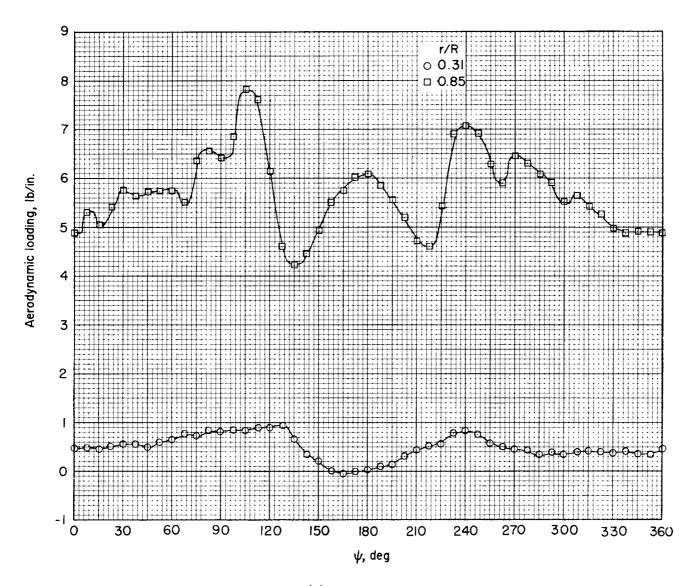


Figure 7.- Variation of section aerodynamic loading with azimuth at various spanwise stations for rear rotor of nonoverlapped rotor system. x/R = 2.03; hovering.



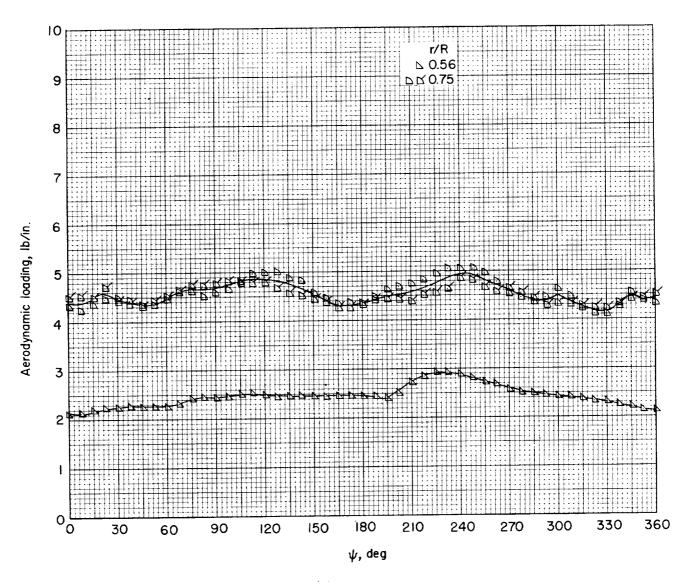
(a) Concluded.

Figure 7.- Continued.



(b) $L_0 = 232.0 \text{ lb.}$

Figure 7.- Continued.



(b) Concluded.

Figure 7.- Concluded.

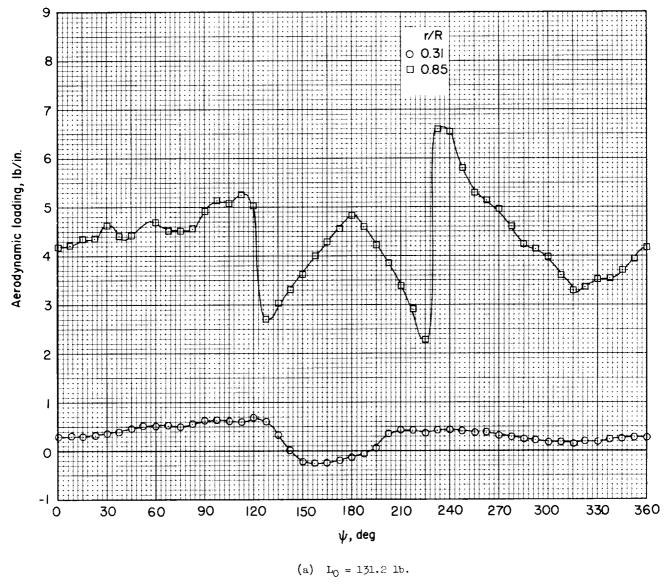
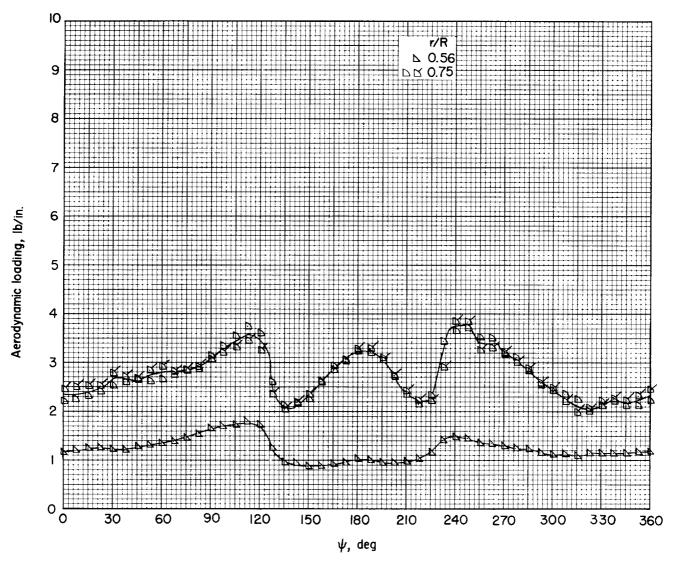
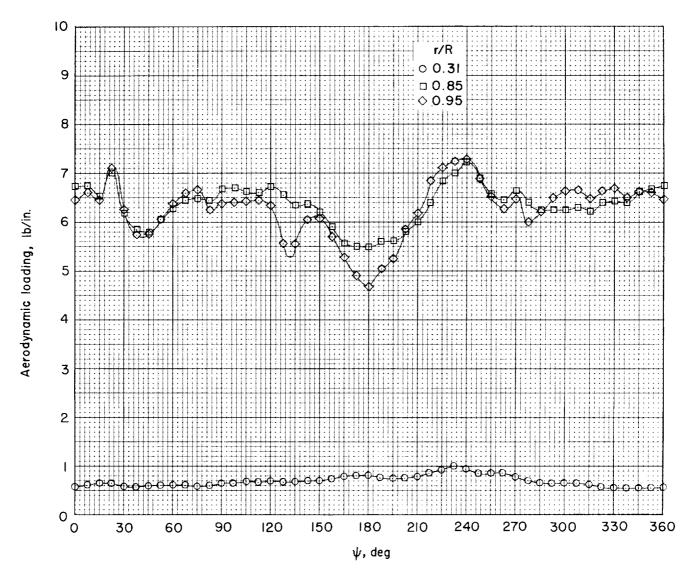


Figure 8.- Variation of section aerodynamic loading with azimuth at various spanwise stations for rear rotor at overlapped rotor system. x/R = 1.23; hovering.



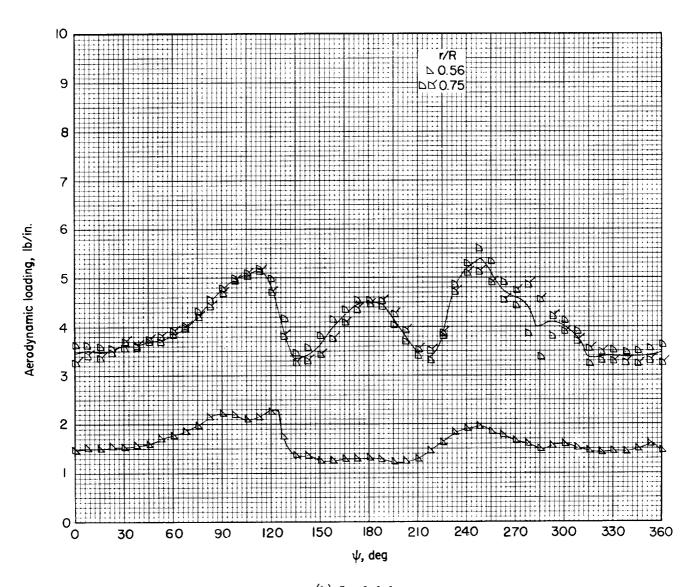
(a) Concluded.

Figure 8. - Continued.



(b) $L_0 = 185.1$ lb.

Figure 8.- Continued.



(b) Concluded.

Figure 8.- Concluded.

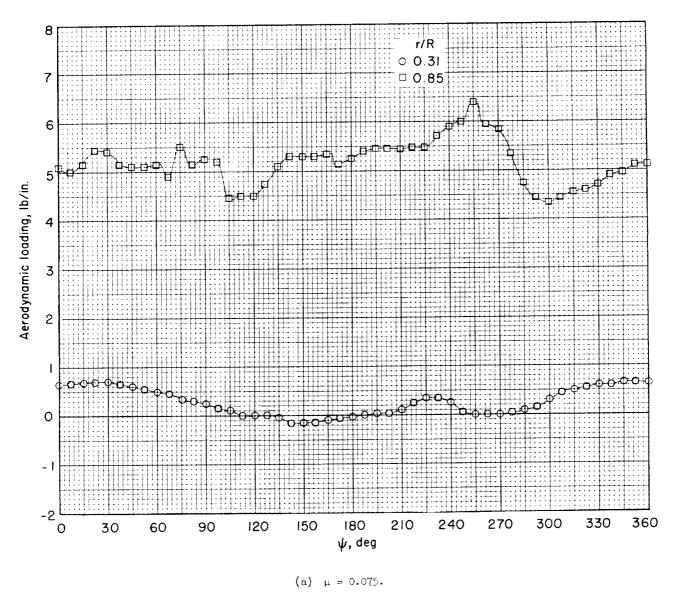
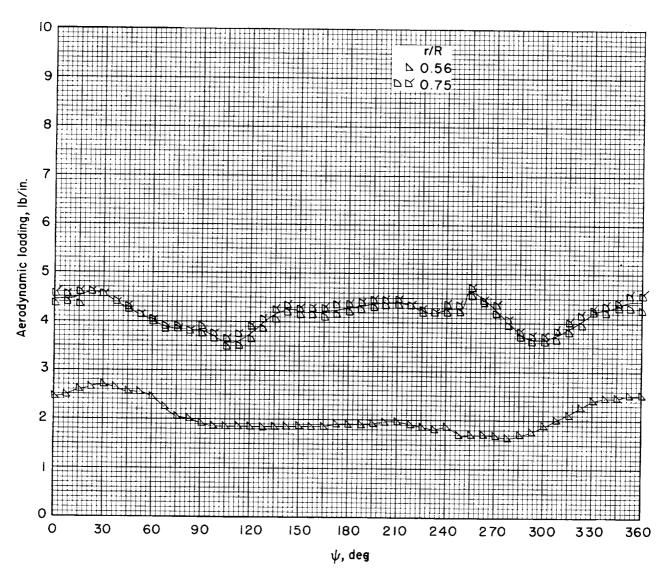
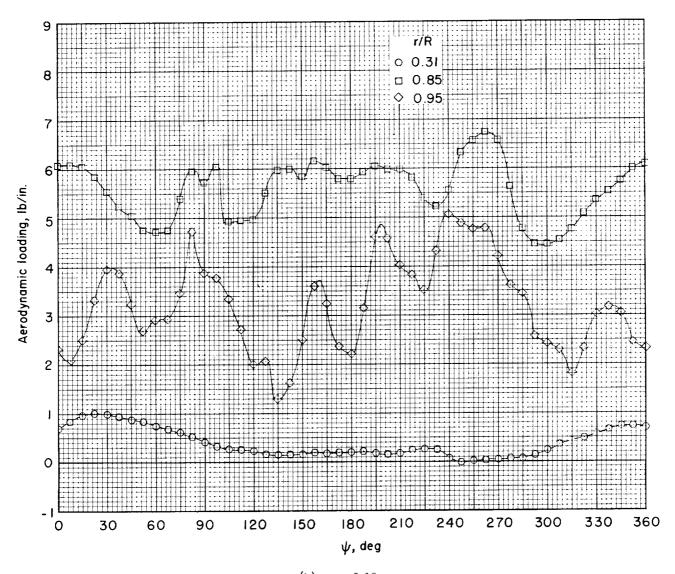


Figure 9.- Variation of section aerodynamic loading with azimuth at various spanwise stations for rear rotor of nonoverlapped rotor system. x/R = 2.03.



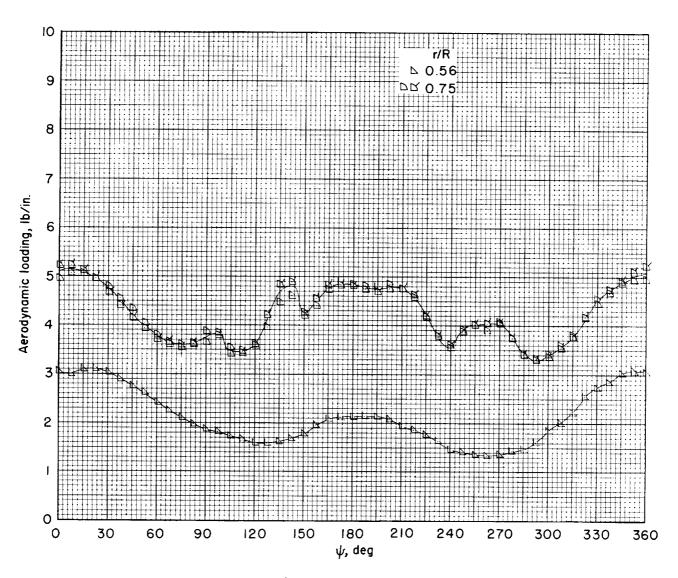
(a) Concluded.

Figure 9.- Continued.



(b) $\mu = 0.10$.

Figure 9.- Continued.



(b) Concluded.

Figure 9.- Continued.

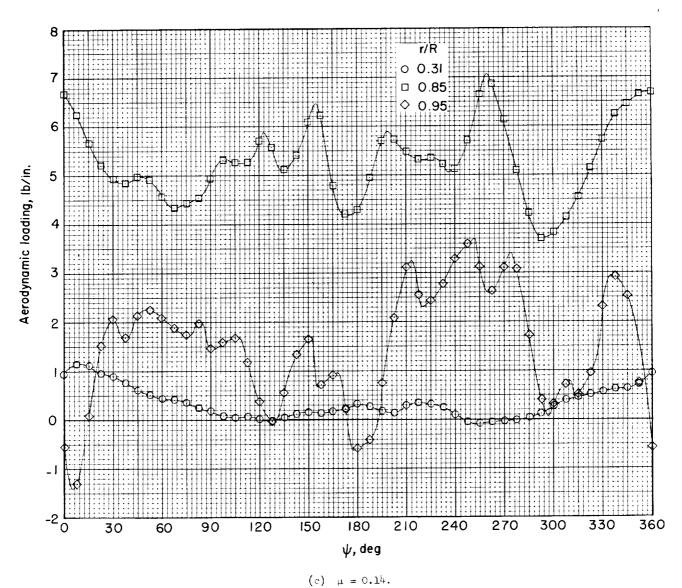
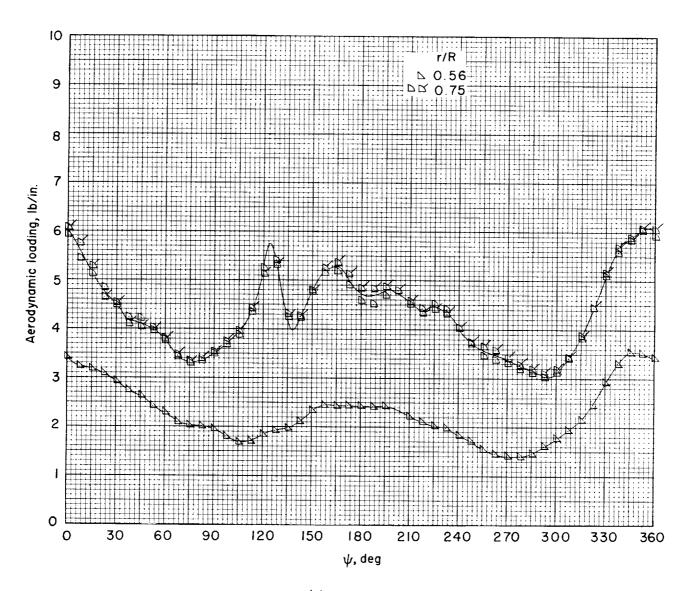
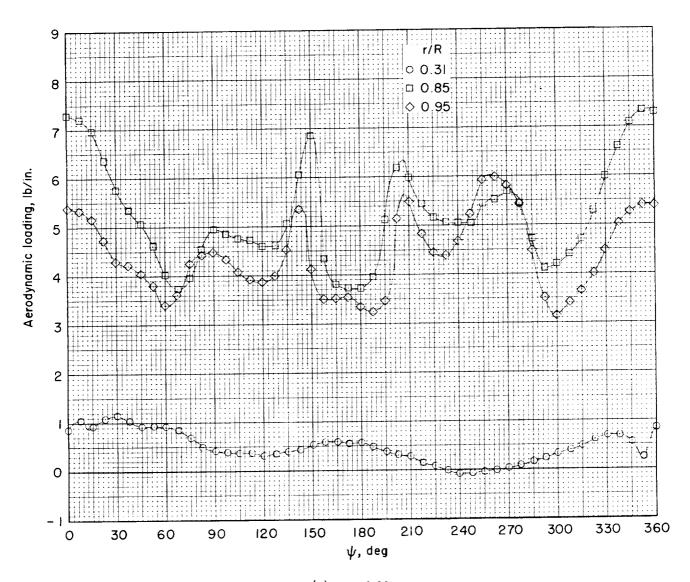


Figure 9.- Continued.



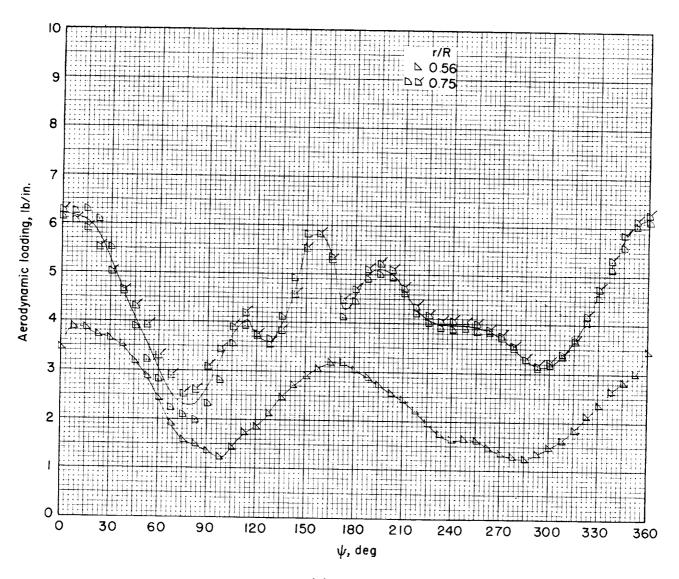
(c) Concluded.

Figure 9.- Continued.



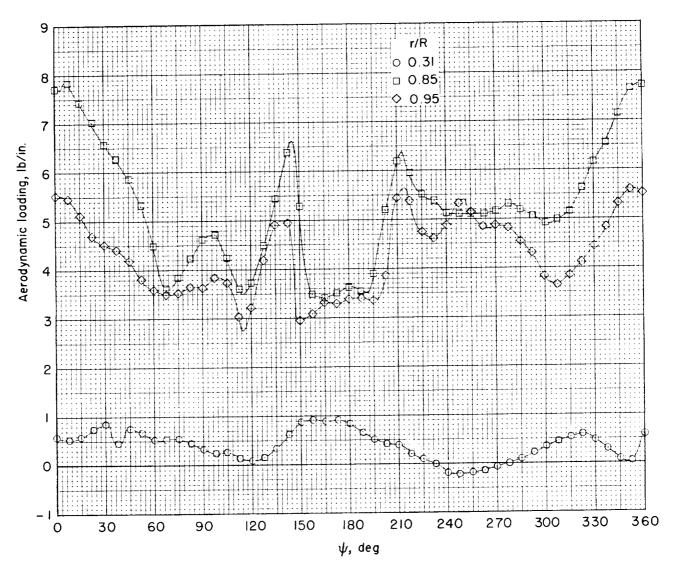
(d) $\mu = 0.19$.

Figure 9.- Continued.



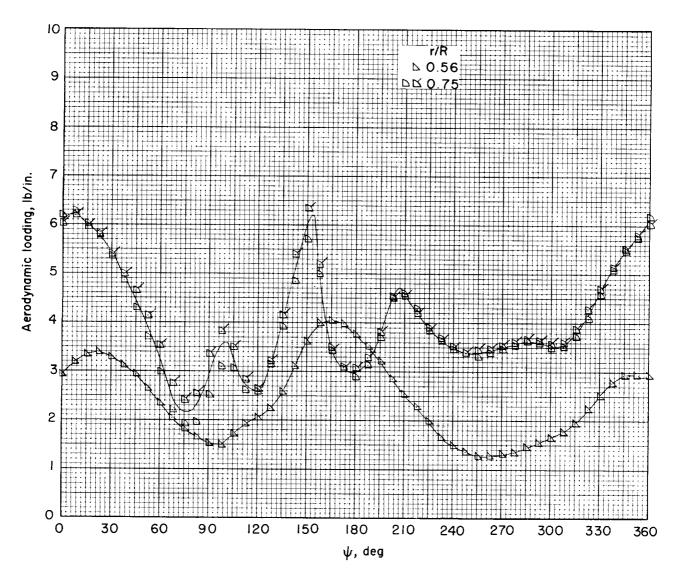
(d) Concluded.

Figure 9.- Continued.



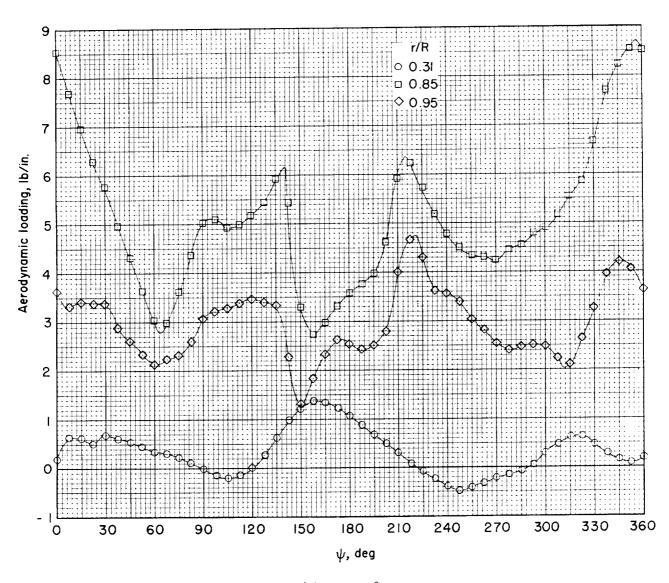
(e) $\mu = 0.24$.

Figure 9.- Continued.



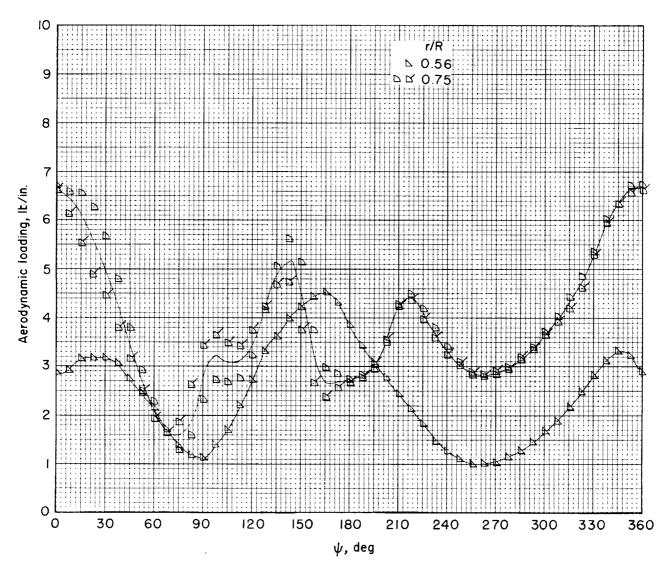
(e) Concluded.

Figure 9.- Continued.



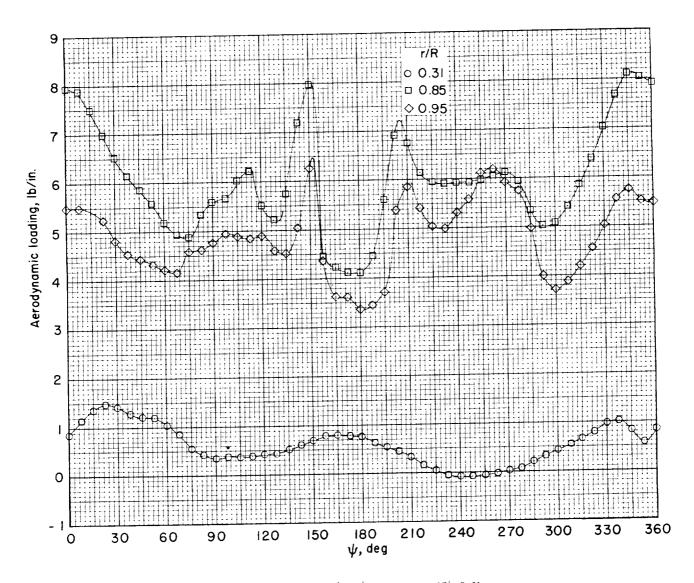
(f) $\mu = 0.28$.

Figure 9.- Continued.



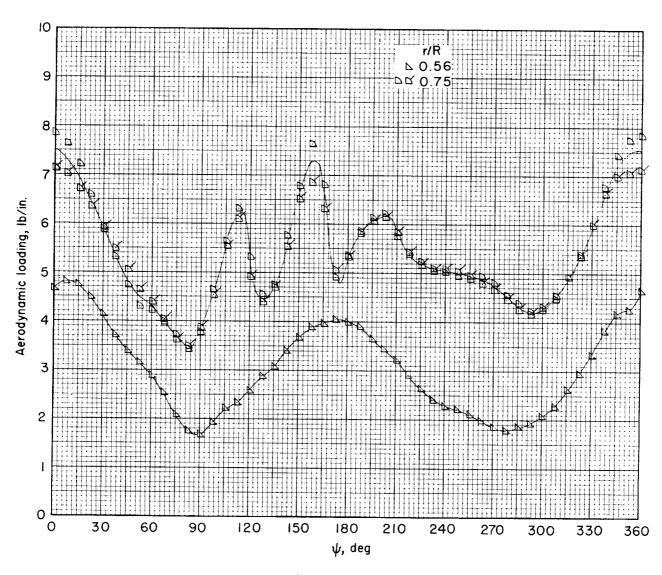
(f) Concluded.

Figure 9.- Concluded.



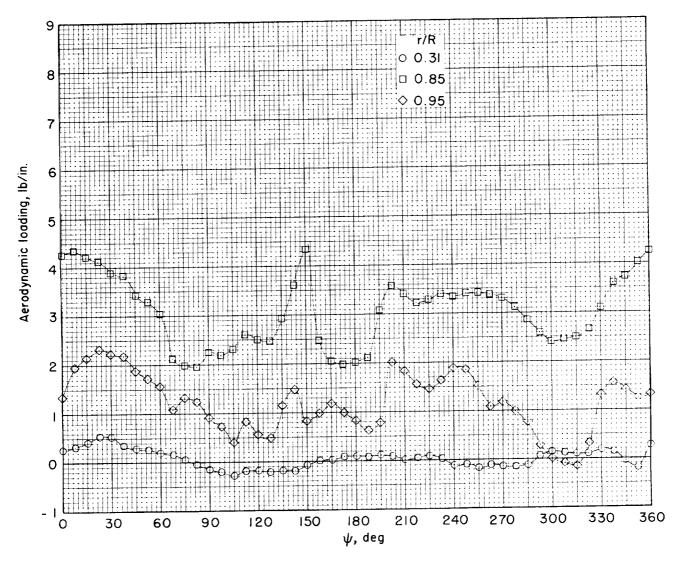
(a) Disk loading = $6 \text{ lb/sq ft; } L_0 = 234.9 \text{ lb.}$

Figure 10.- Variation of section aerodynamic loading with azimuth at various spanwise stations for rear rotor of nonoverlapped rotor system for special conditions. x/R = 2.03. $\mu = 0.19$.



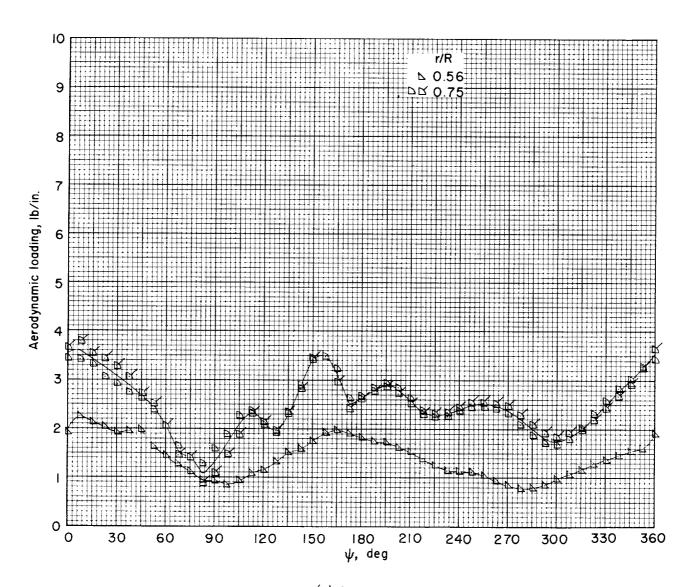
(a) Concluded.

Figure 10.- Continued.



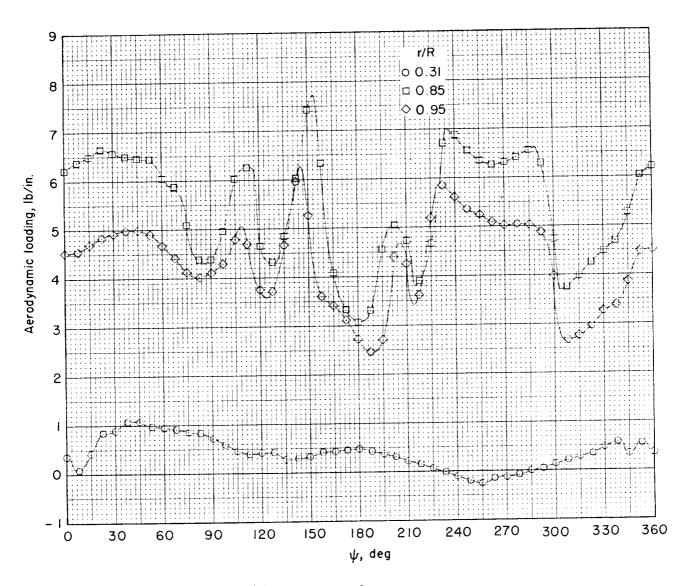
(b) Disk loading = 3 lb/sq ft; $L_{\rm O}$ = 100.5 lb.

Figure 10. - Continued.



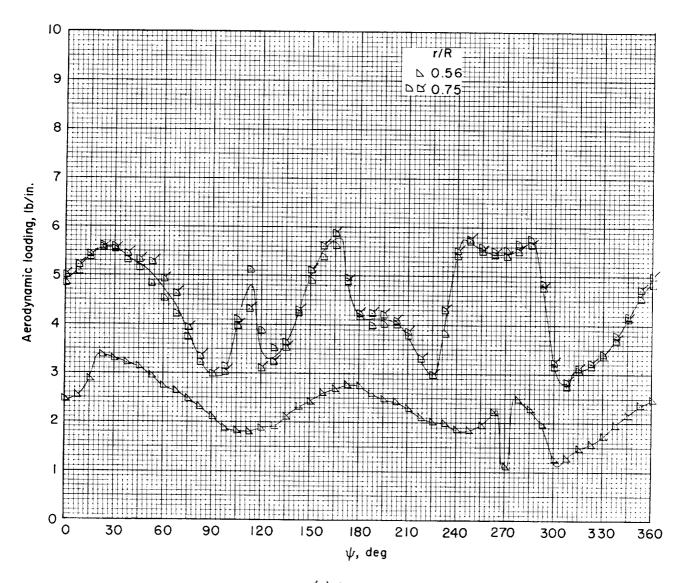
(b) Concluded.

Figure 10. - Continued.



(c) Yaw angle = 10° ; L_{0} = 192.3 lb.

Figure 10.- Continued.



(c) Concluded.

Figure 10.- Concluded.

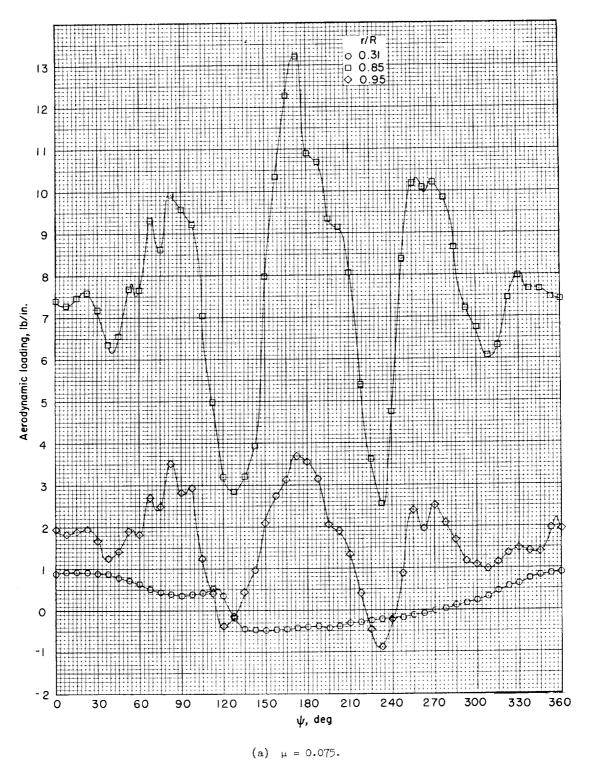
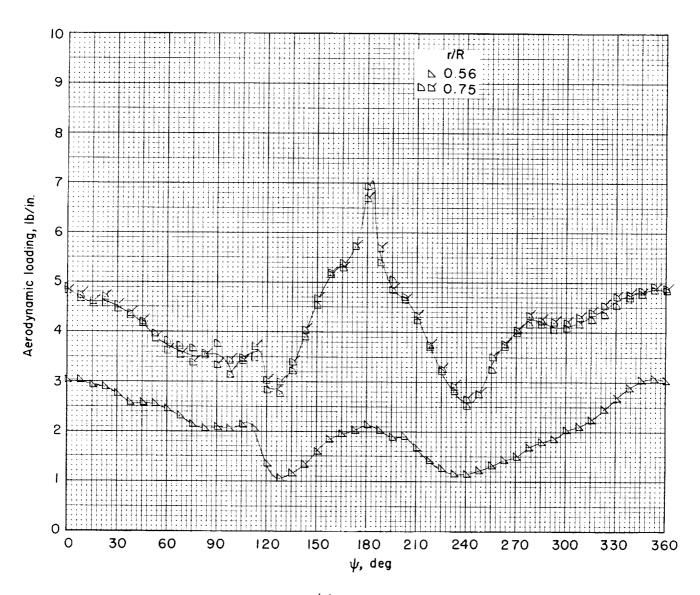
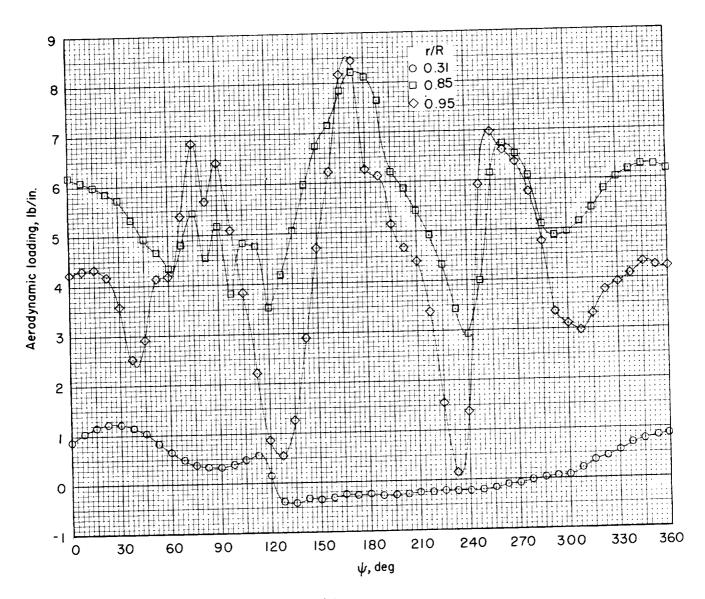


Figure 11.- Variation of section aerodynamic loading with azimuth at various spanwise stations for rear rotor of overlapped rotor system. x/R = 1.23.



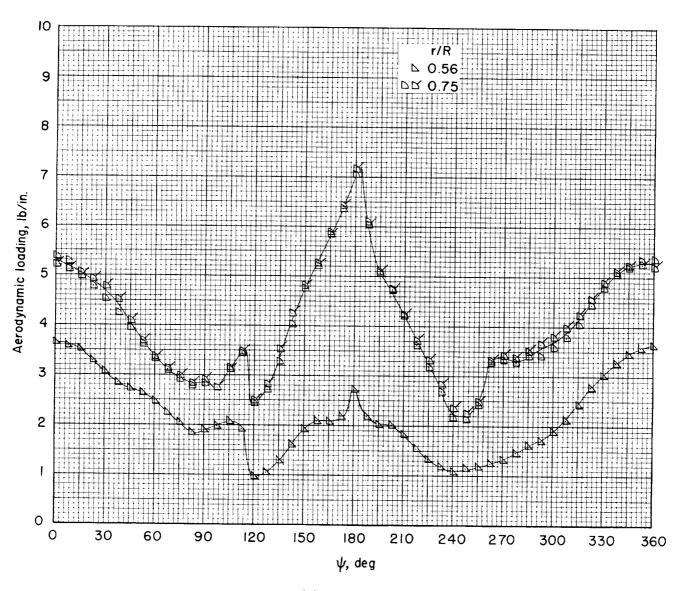
(a) Concluded.

Figure 11.- Continued.



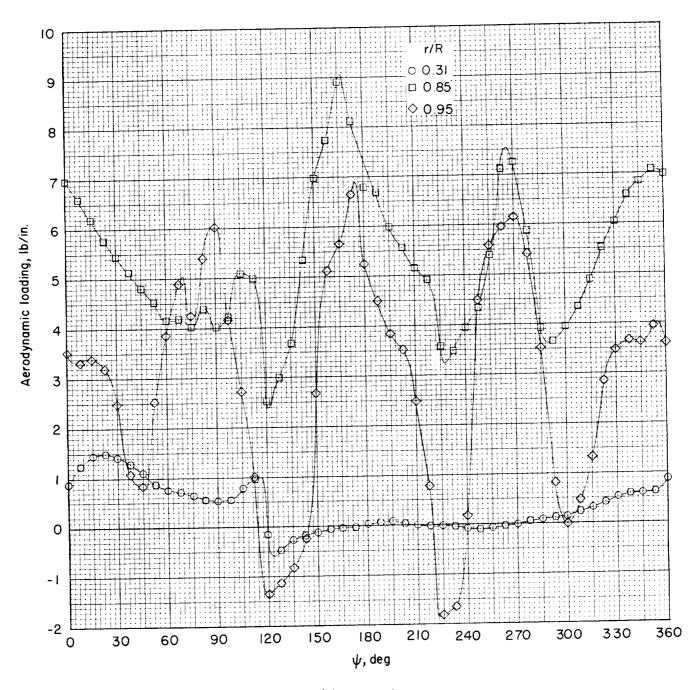
(b) $\mu = 0.10$.

Figure 11.- Continued.



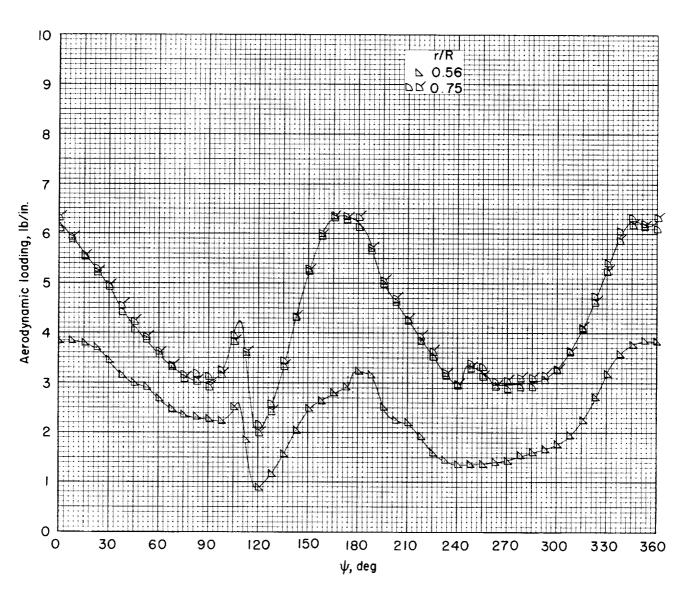
(b) Concluded.

Figure 11. - Continued.



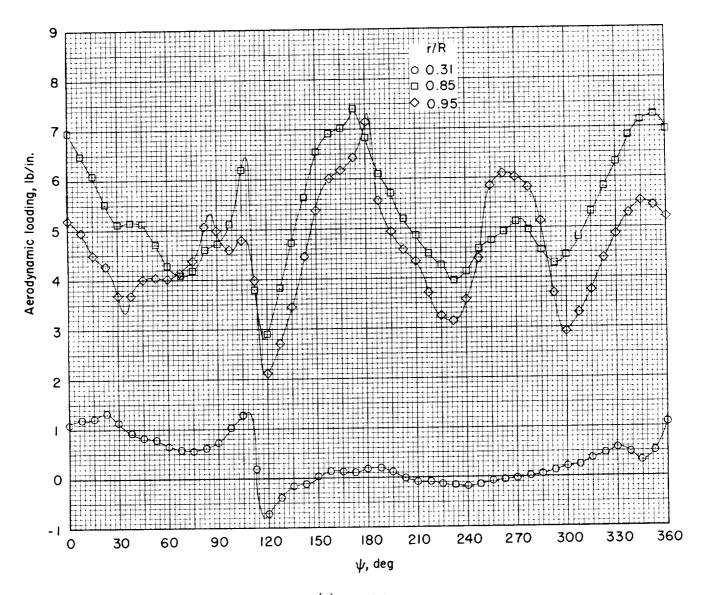
(e) $\mu = 0.14$.

Figure 11.- Continued.



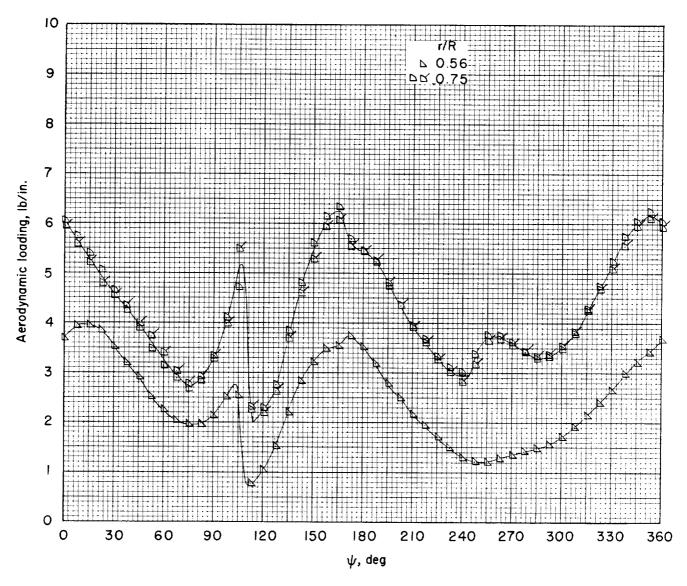
(c) Concluded.

Figure 11.- Continued.



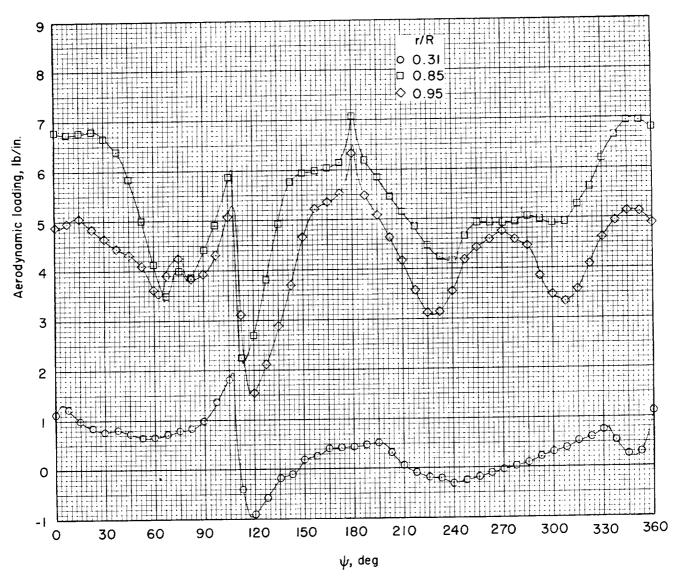
(d) $\mu = 0.19$.

Figure 11. - Continued.



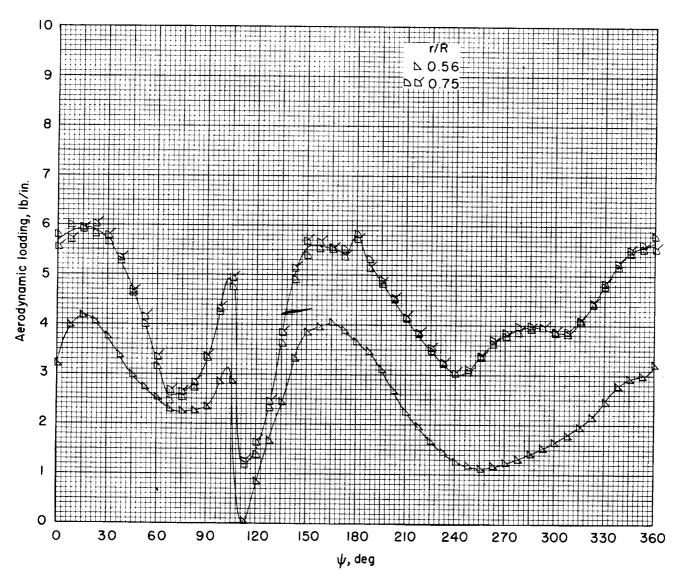
(d) Concluded.

Figure 11. - Continued.



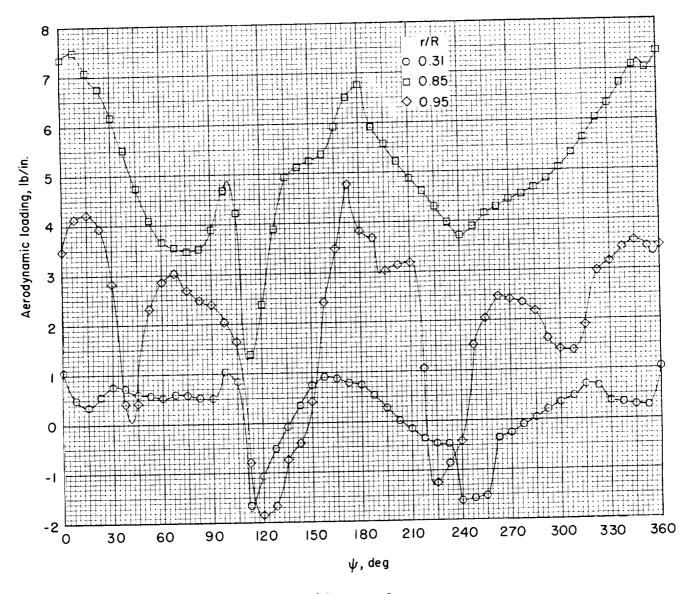
(e) $\mu = 0.24$.

Figure 11.- Continued.



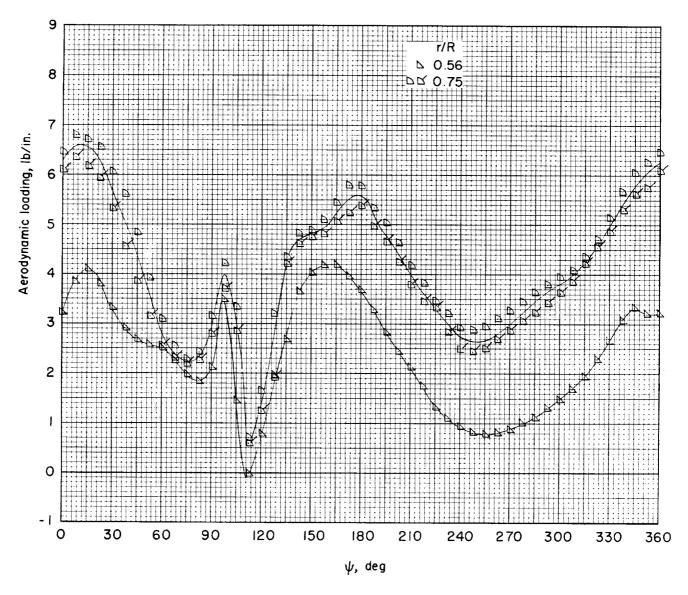
(e) Concluded.

Figure 11.- Continued.



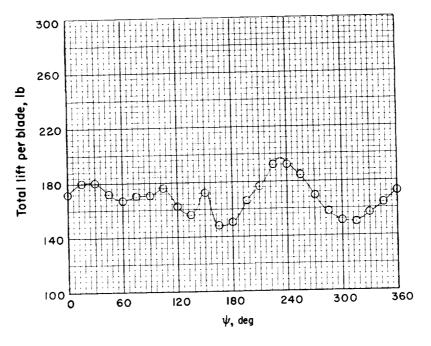
(f) $\mu = 0.28$.

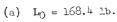
Figure 11.- Continued.

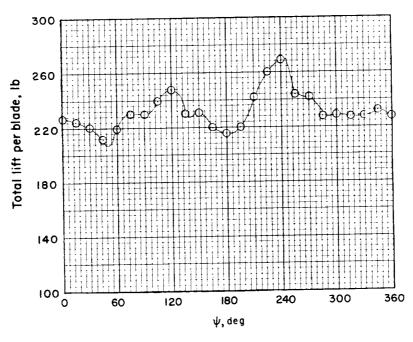


(f) Concluded.

Figure 11.- Concluded.

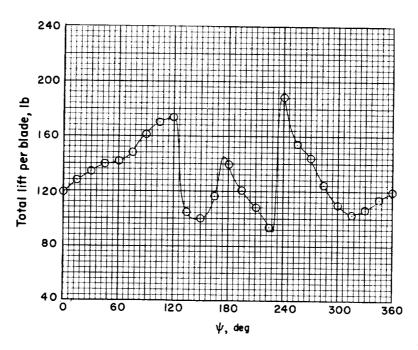


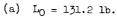




(b) $L_0 = 232.0 \text{ lb.}$

Figure 12.- Variation of total blade lift with azimuth for rear rotor of nonoverlapped rotor system in hovering. x/R=2.03.





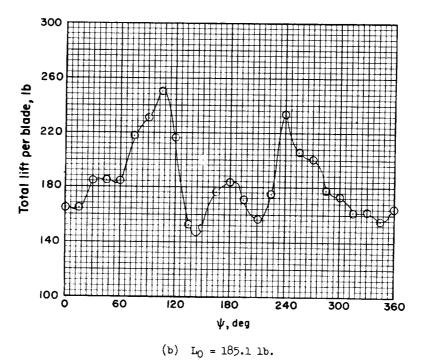
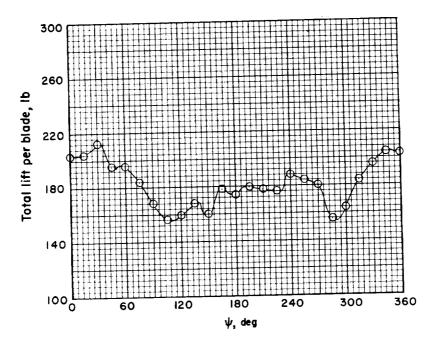


Figure 13.- Variation of total blade lift with azimuth for rear rotor of overlapped rotor system in hovering. x/R = 1.23.



(a) $\mu = 0.075$.

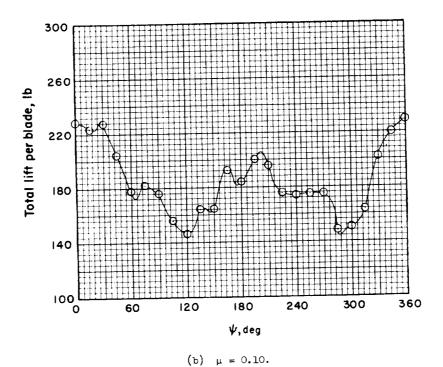
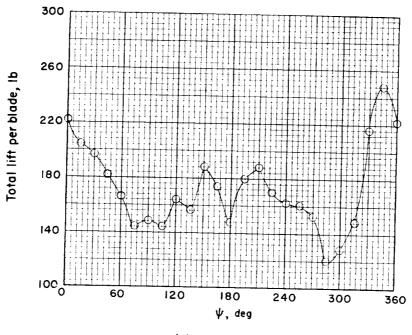
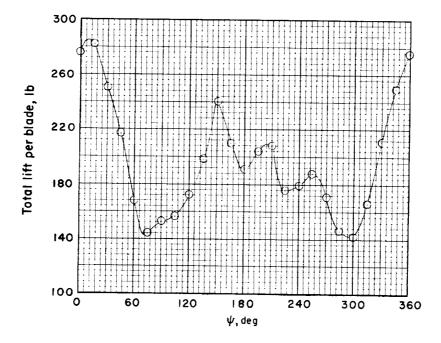


Figure 14.- Variation of total blade lift with azimuth for rear rotor of nonoverlapped rotor system. x/R = 2.03.

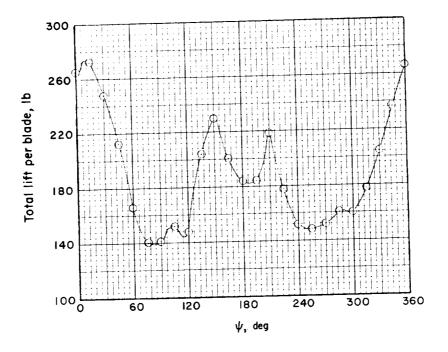




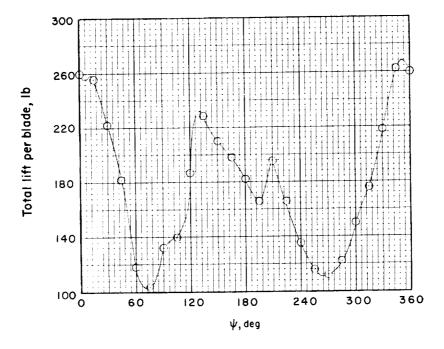


(d) $\mu = 0.19$.

Figure 14.- Continued.

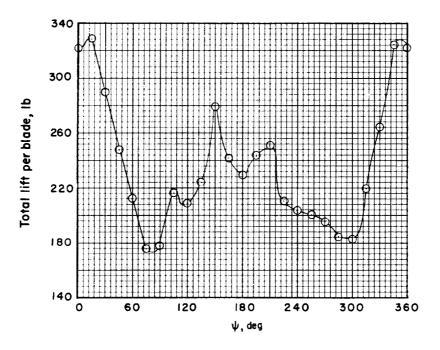


(e) $\mu = 0.24$.

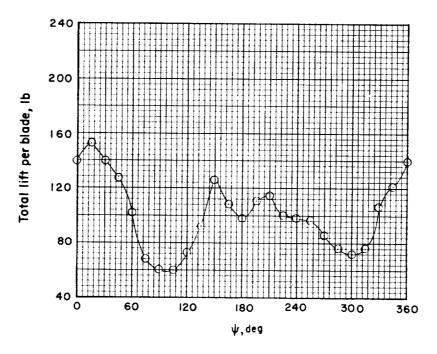


(f) $\mu = 0.28$.

Figure 14.- Concluded.

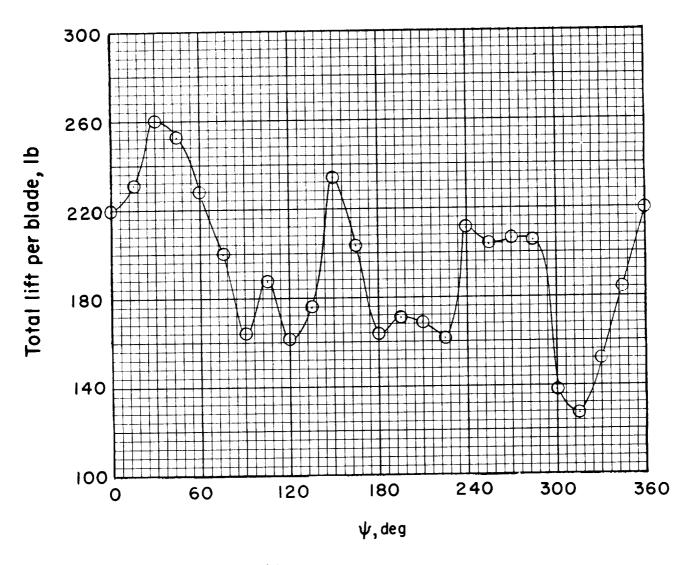


(a) Disk loading = 6 lb/sq ft; $L_{\rm O}$ = 234.9 lb.

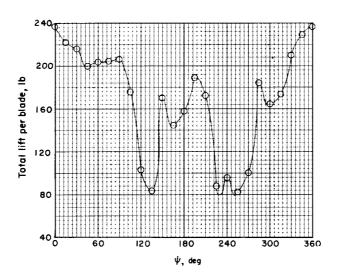


(b) Disk loading = 3 lb/sq ft; I_0 = 100.5 lb.

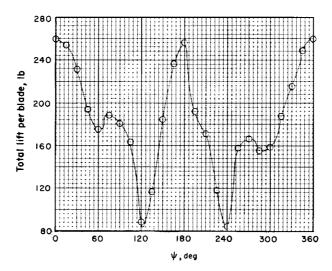
Figure 15.- Variation of total blade lift with azimuth for rear rotor of nonoverlapped rotor system for special conditions. μ = 0.19; x/R = 2.03.



(c) Yaw angle = 10° ; $L_{\rm O}$ = 192.3 lb. Figure 15.- Concluded.



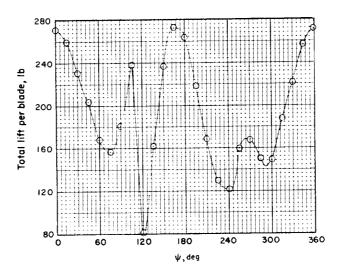




(b) $\mu = 0.10$.

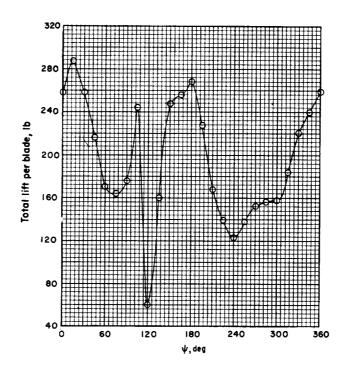
Figure 16.- Variation of total blade lift with azimuth for rear rotor of overlapped rotor system. x/R = 1.23.

(c) $\mu = 0.14$.

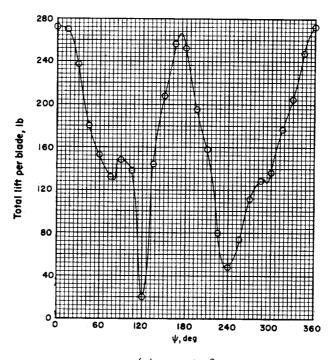


(d) $\mu = 0.19$.

Figure 16.- Continued.



(e) $\mu = 0.24$.



(f) $\mu = 0.28$.

Figure 16.- Concluded.